



*In memoriam* Sofija Kanopkaitė (1926 – 2024)

# MATEMATINIO MODELIAVIMO UŽDAVINYS ONKOLOGIJOJE

nr.1

COPYRIGHT ©

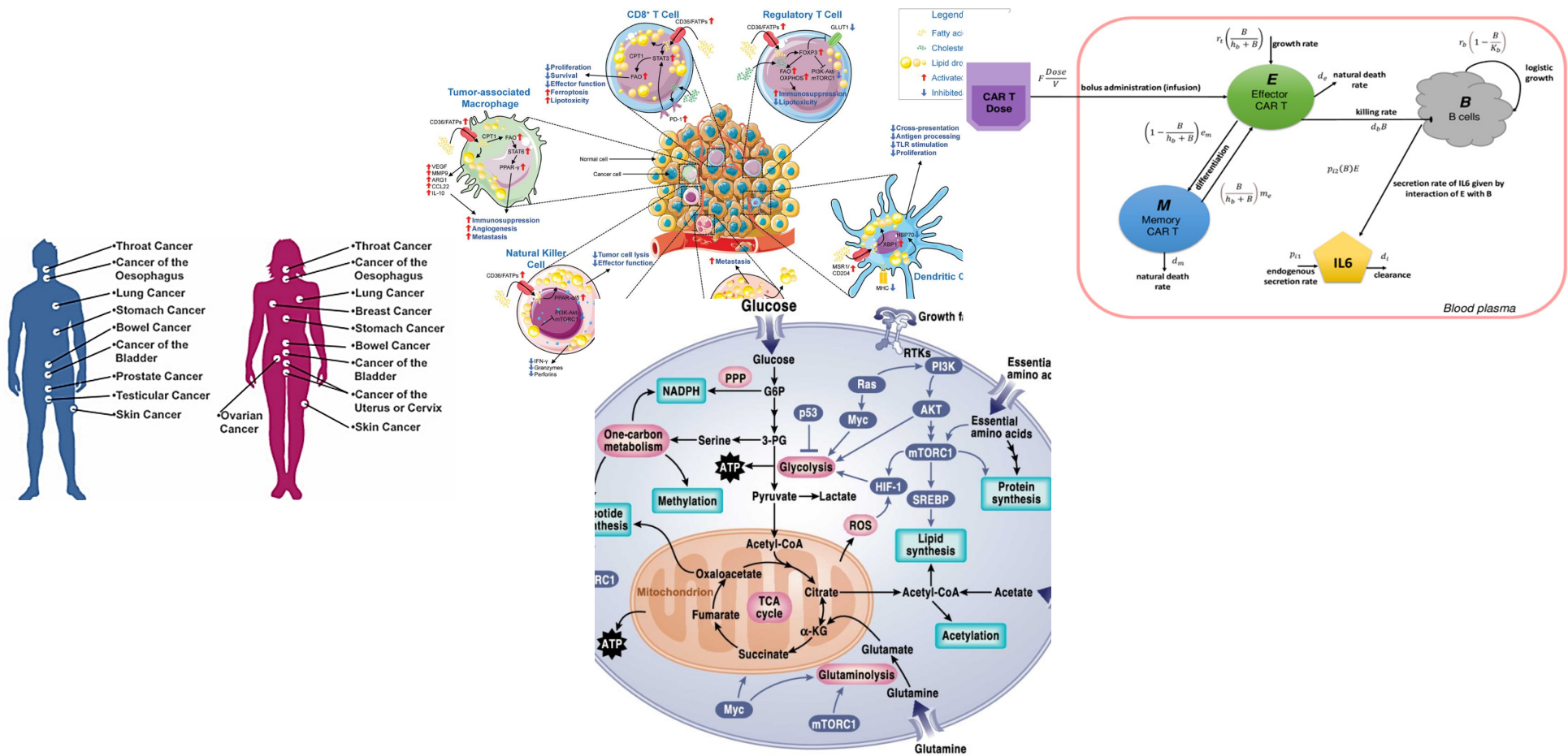
Kęstutis K.Urba

*USA NCI - The Ras initiative - international project*

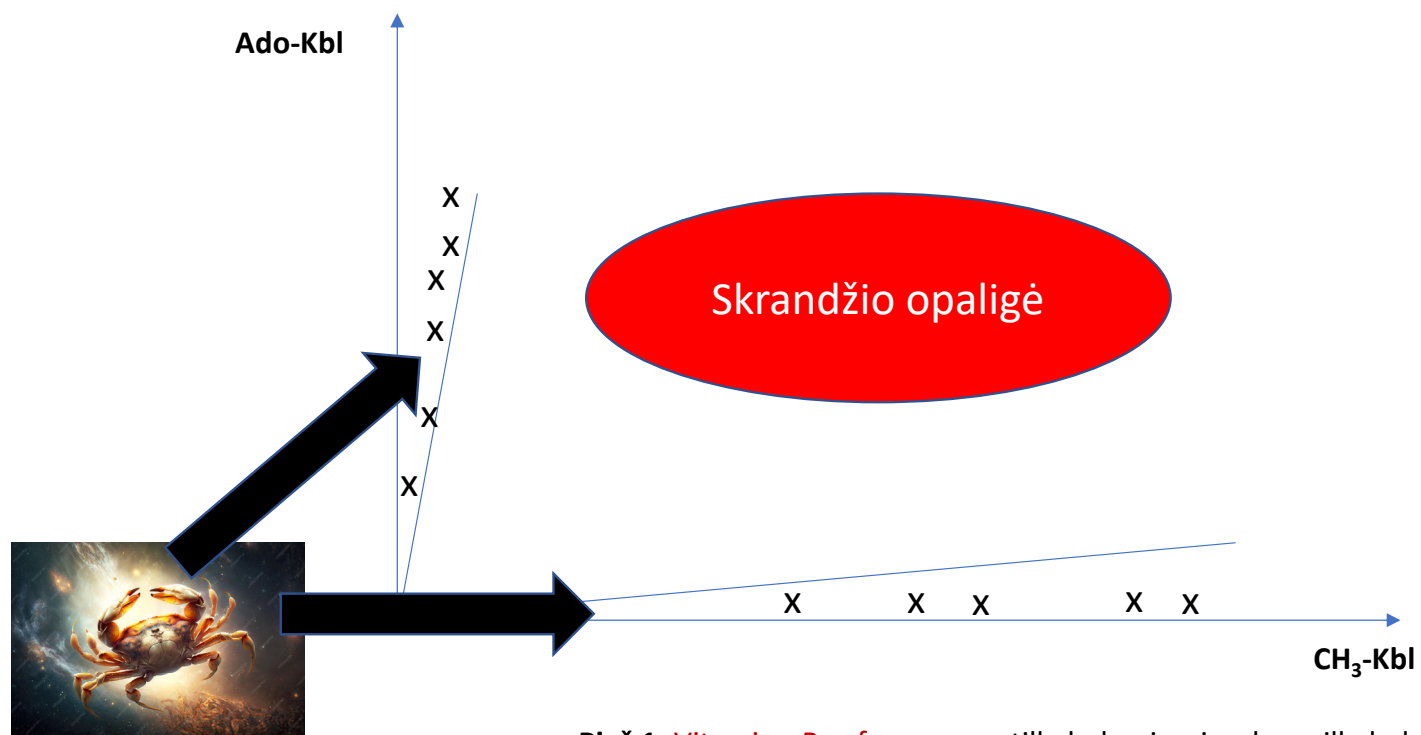
2025 m. rugsėjo mėn. 23 d. VGTU MMK

urbascience@gmail.com

# JVADAS: modeliuotino objekto sudėtingumas

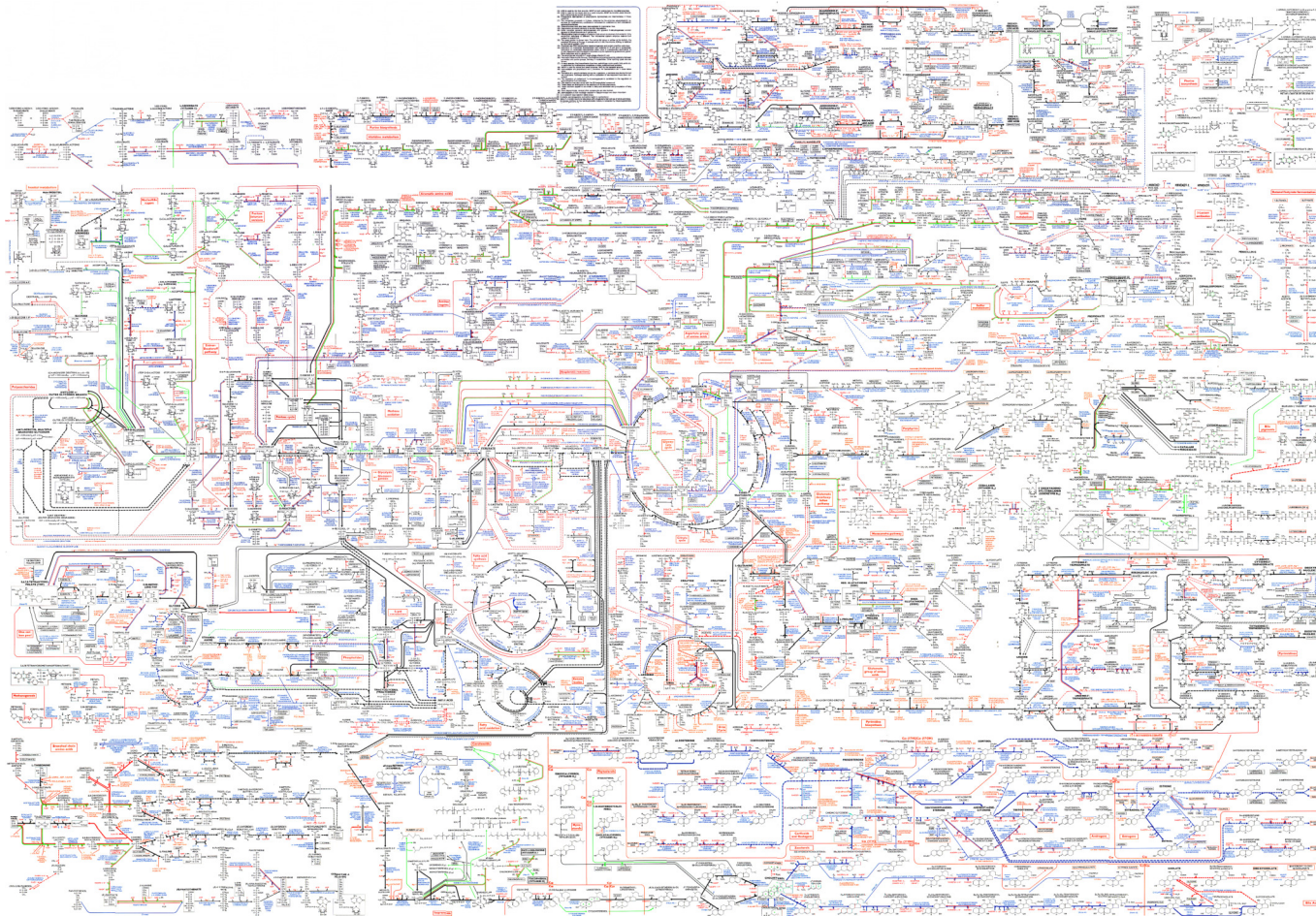


Empirinių duomenų analizės būdu gautas diagnostinis algoritmas - 1989 metai,  
išradimas 1992 ( akad.S.Kanopkaitė ... K.Urba)

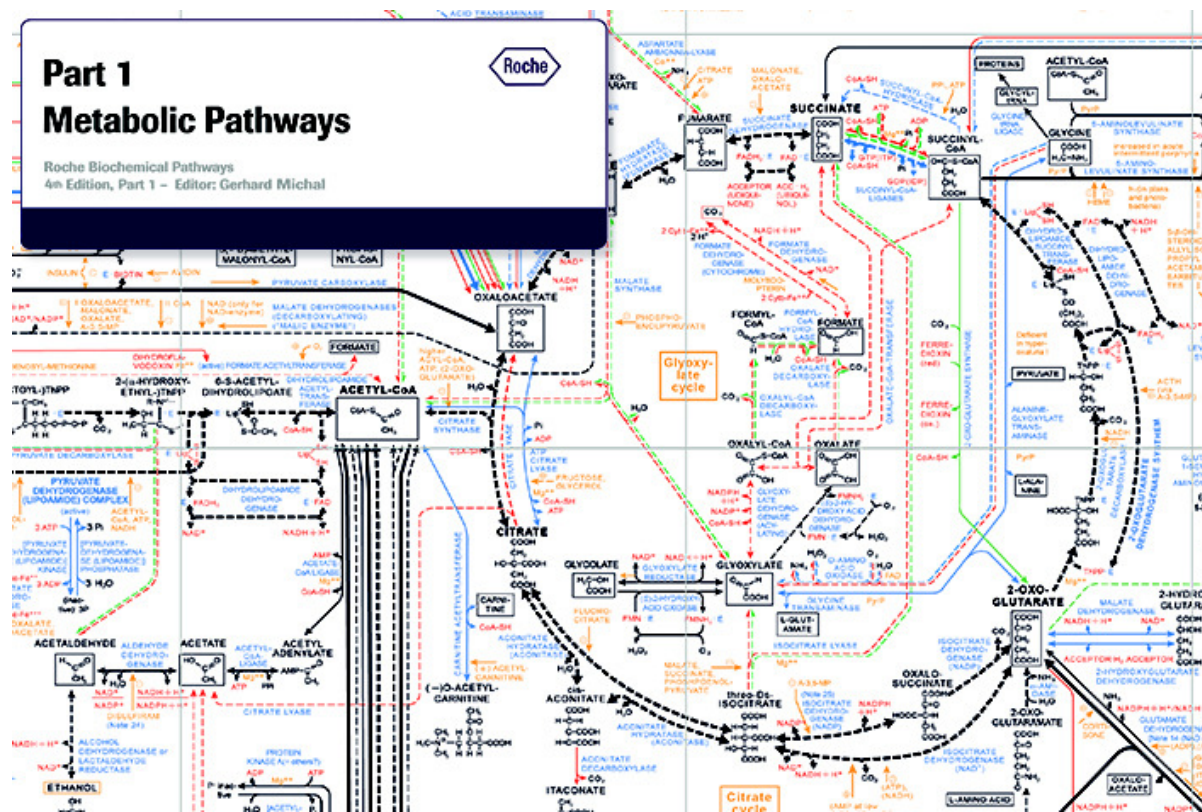


**Pieš 1. Vitamino B<sub>12</sub> formų** – metilkobalamino ir adenzilkobalamino kraujo ląstelėse pasiskirstymas žmonių sergančių vėžiu ( x ) bei skrandžio opalige

# Medžiagų apykaitos žemėlapis

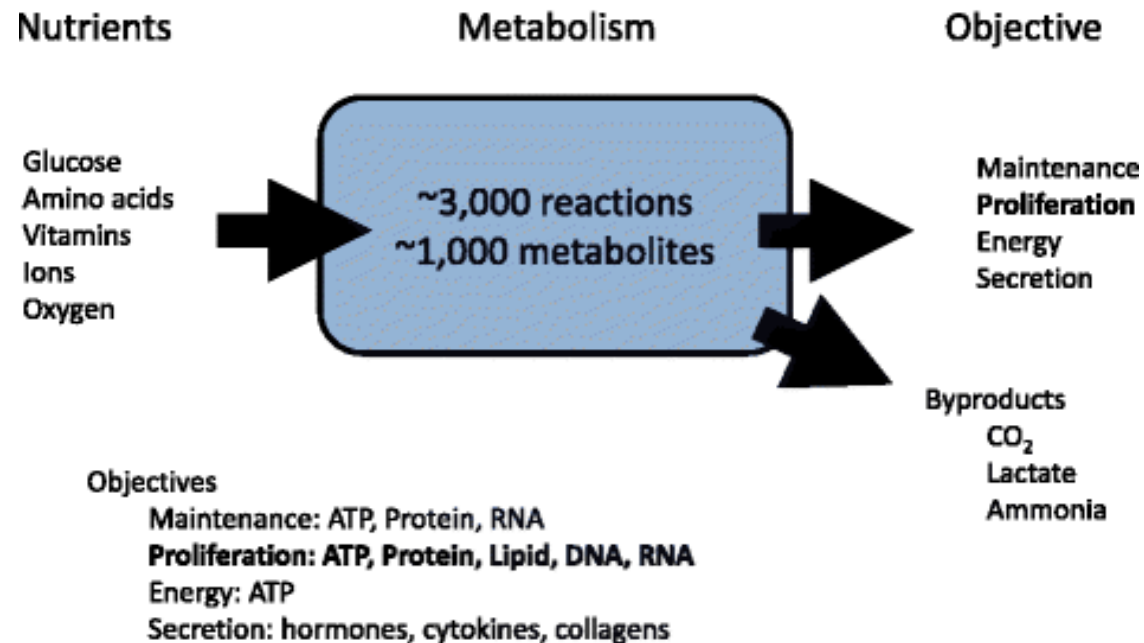


# ROCHE žemėlapis raiškesniame mastelyje

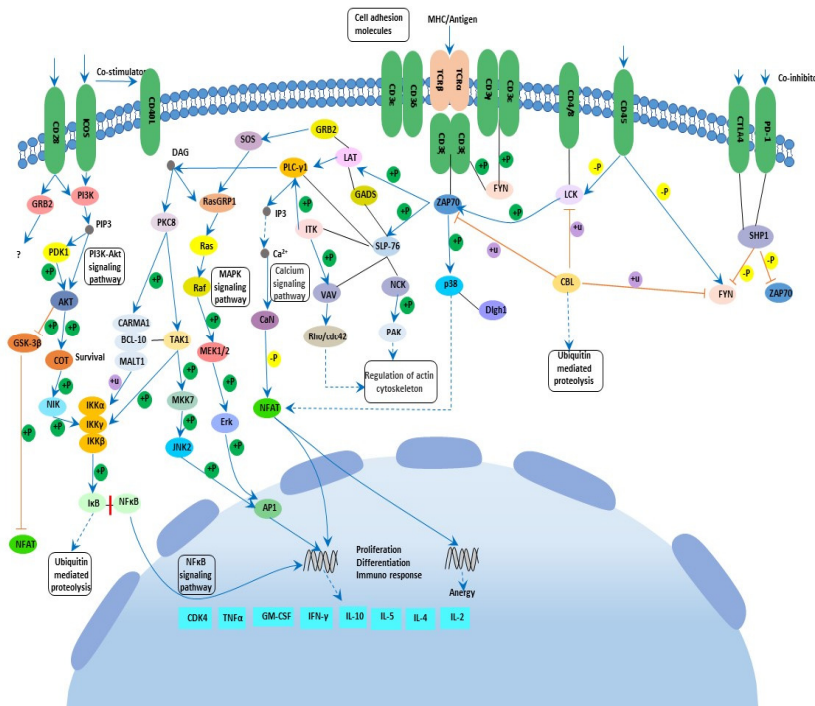


## Tyrinėjamos apykaitos apimtys ([Elke Katrin Markert, Alexei Vazquez, 2015](#))

### Genome scale model of human cell metabolism



# Signalų perdavimas transkripcijai nuo membranos



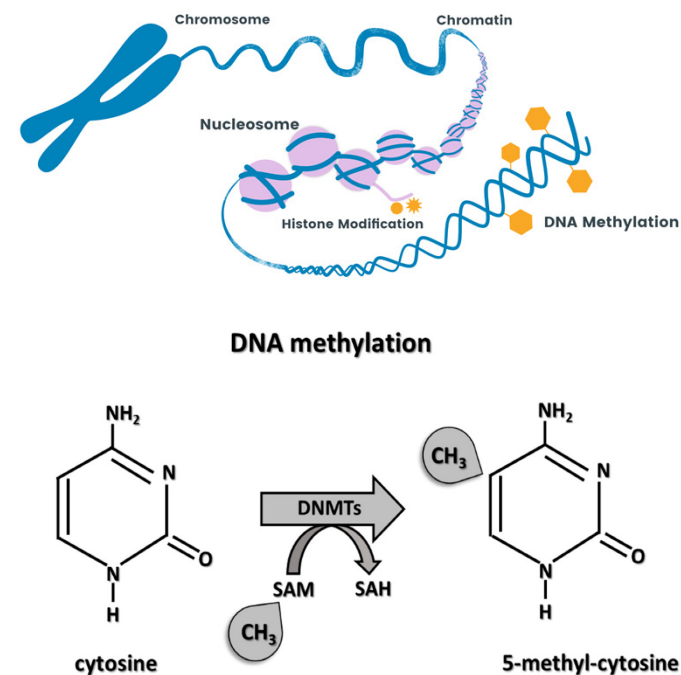
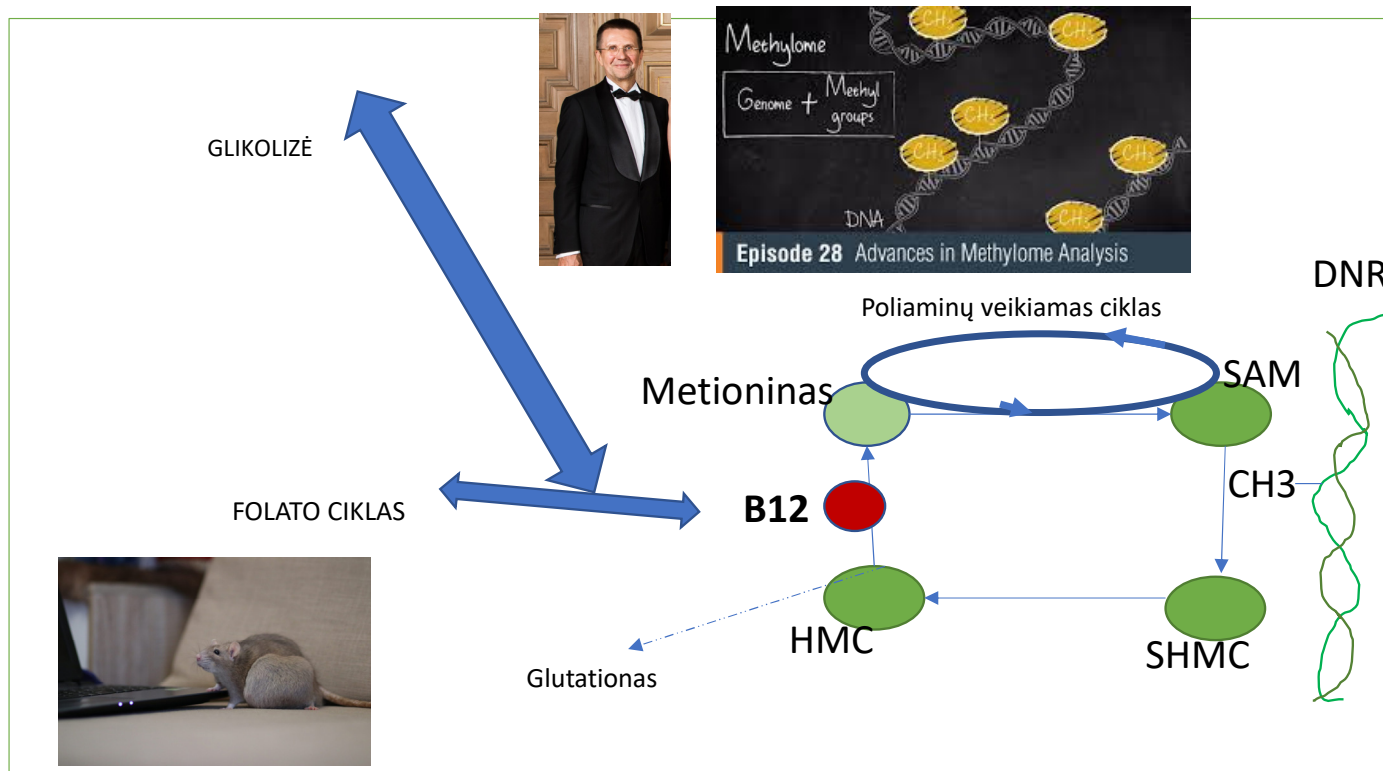
1. Ekspozomika (Ex),
2. Genomika (G),
3. Signalomika (S),
4. Cistromika (C),
5. Transkriptomika (TR),
6. Proteomika (P),
7. Lipidomika (L) ([\*Smirnov D. et al. 2021\*](#)),
8. Metalomika (Mtl) ([\*Zhang Y., et al, 2022\*](#)),  
([\*Wolters DA., et al, 2012\*](#))
9. Metabolomika (M)
10. Epigenomika (Ep),
11. Imunomika (Im) ([\*Nevedomskaya E, Haendler B. 2022\*](#))
12. Fliuksomika (F)

$$\{TUMOR^{OEx}\}_t = U_k U_i f_{k,ij}(Ex_{\xi_1}, G(K)_{\xi_2}, S(K)_{\xi_3}, C(K)_{\xi_4}, Tr(K)_{\xi_5}, P(K)_{\xi_6}, L(K)_{\xi_7}, Mtl(K)_{\xi_8}, M(K)_{\xi_9}, F(K)_{\xi_{10}}, Ep(K)_{\xi_{11}}, I_{\xi_{12}})$$

# I dalis. Vienanglių fragmentų – „1C“ apykaita ir modeliavimas: Duke universitetas, Kornelio universitetas, Trento (Italija), Bordo (Prancūzija), Brisbenas (Australija)...

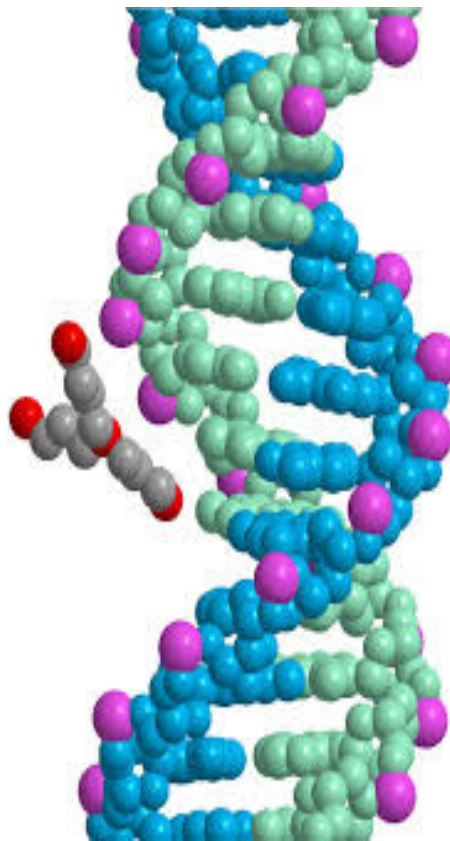
1. Ducker GS, Rabinowitz JD. One-Carbon Metabolism in Health and Disease. *Cell Metab.* 2017 Jan 10;25(1):27-42. doi: 10.1016/j.cmet.2016.08.009. Epub 2016 Sep 15. PMID: 27641100; PMCID: PMC5353360. <https://pubmed.ncbi.nlm.nih.gov/27641100/>
2. Clare CE, Brassington AH, Kwong WY, Sinclair KD. One-Carbon Metabolism: Linking Nutritional Biochemistry to Epigenetic Programming of Long-Term Development. *Annu Rev Anim Biosci.* 2019 Feb 15;7:263-287. doi: 10.1146/annurev-animal-020518-115206. Epub 2018 Nov 9. PMID: 30412672. <https://pubmed.ncbi.nlm.nih.gov/30412672/>
3. Nijhout HF, Reed MC, Budu P, Ulrich CM. A mathematical model of the folate cycle: new insights into folate homeostasis. *J Biol Chem.* 2004 Dec 31;279(53):55008-16. doi: 10.1074/jbc.M410818200. Epub 2004 Oct 20. PMID: 15496403. <https://pubmed.ncbi.nlm.nih.gov/15496403/>
4. Reed MC, Nijhout HF, Neuhauser ML, Gregory JF 3rd, Shane B, James SJ, Boynton A, Ulrich CM. A mathematical model gives insights into nutritional and genetic aspects of folate-mediated one-carbon metabolism. *J Nutr.* 2006 Oct;136(10):2653-61. doi: 10.1093/jn/136.10.2653. PMID: 16988141. <https://pubmed.ncbi.nlm.nih.gov/16988141/>
5. Ulrich CM, Reed MC, Nijhout HF. Modeling folate, one-carbon metabolism, and DNA methylation. *Nutr Rev.* 2008 Aug;66 Suppl 1:S27-30. doi: 10.1111/j.1753-4887.2008.00062.x. PMID: 18673484. <https://pubmed.ncbi.nlm.nih.gov/18673484/>  
<https://sites.duke.edu/metabolism/files/2015/11/08nutrrev.pdf>
6. Duncan TM, Reed MC, Nijhout HF. A population model of folate-mediated one-carbon metabolism. *Nutrients.* 2013 Jul 5;5(7):2457-74. doi: 10.3390/nu5072457. PMID: 23857220; PMCID: PMC3738981. <https://pmc.ncbi.nlm.nih.gov/articles/PMC3738981/>
7. Sadre-Marandi F, Dahdoul T, Reed MC, Nijhout HF. Sex differences in hepatic one-carbon metabolism. *BMC Syst Biol.* 2018 Oct 24;12(1):89. doi: 10.1186/s12918-018-0621-7. PMID: 30355281; PMCID: PMC6201565. <https://pubmed.ncbi.nlm.nih.gov/30355281/>
8. Kim R, Nijhout HF, Reed MC. One-carbon metabolism during the menstrual cycle and pregnancy. *PLoS Comput Biol.* 2021 Dec 16;17(12):e1009708. doi: 10.1371/journal.pcbi.1009708. PMID: 34914693; PMCID: PMC8741061. <https://pubmed.ncbi.nlm.nih.gov/34914693/>
9. Scotti M, Stella L, Shearer EJ, Stover PJ. Modeling cellular compartmentation in one-carbon metabolism. *Wiley Interdiscip Rev Syst Biol Med.* 2013 May-Jun;5(3):343-65. doi: 10.1002/wsbm.1209. Epub 2013 Feb 13. PMID: 23408533; PMCID: PMC4437664. <https://pmc.ncbi.nlm.nih.gov/articles/PMC4437664/>
10. Mazat JP. One-carbon metabolism in cancer cells: a critical review based on a core model of central metabolism. *Biochem Soc Trans.* 2021 Feb 26;49(1):1-15. doi: 10.1042/BST20190008. PMID: 33616629. <https://pubmed.ncbi.nlm.nih.gov/33616629/>

Vitaminas B12-Metionino ciklas: „One-carbon Metabolism at the Root of Carcinogenesis“ ([Adam Rosenzweig](#), [John Blenis](#), and [Ana P. Gomes](#), Meyer Cancer Center, NYC. Beyond the Warburg Effect: How Do Cancer Cells Regulate One-Carbon Metabolism?, 2018)

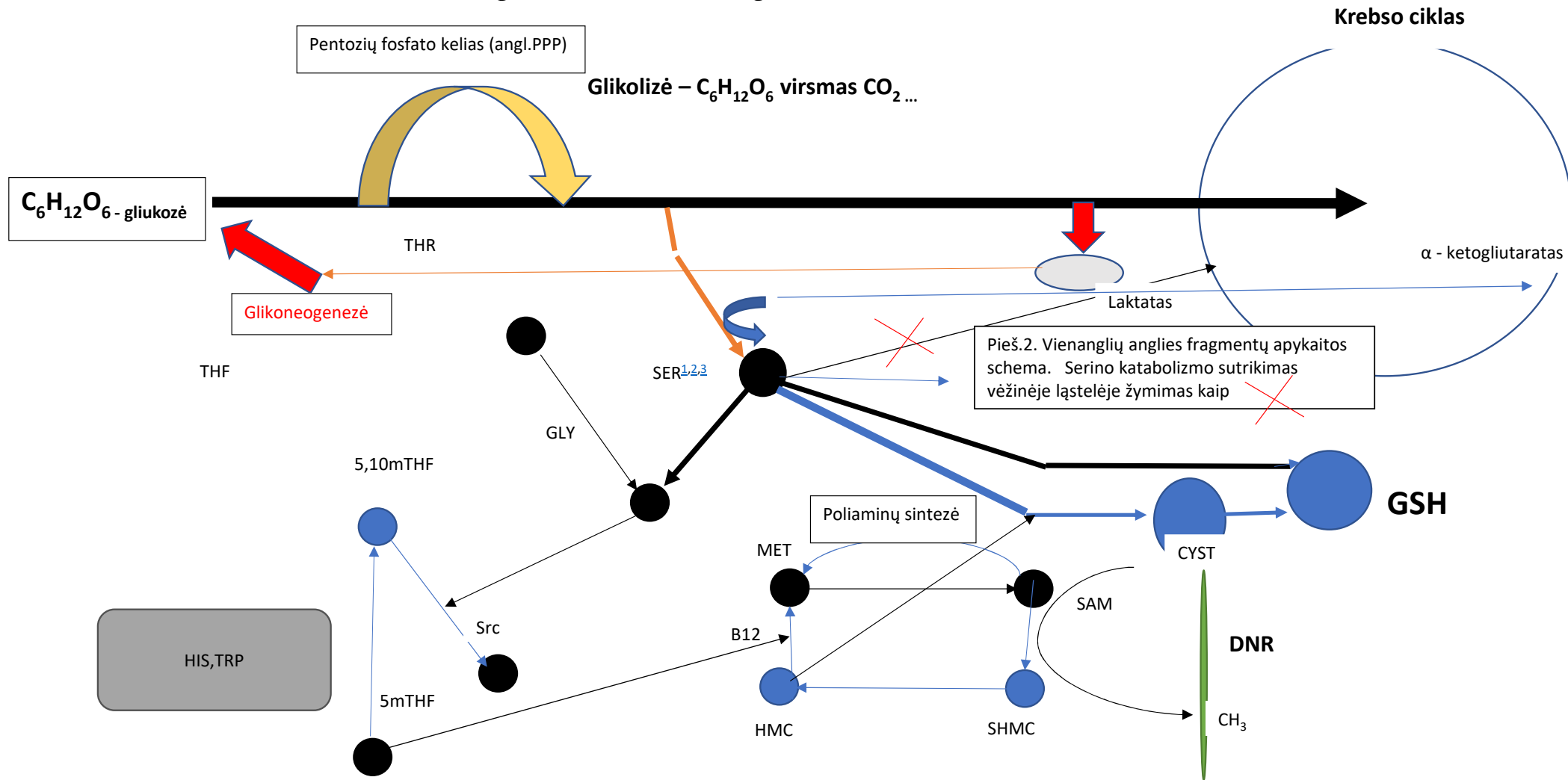


**CH3** - Vienanglių fragmentų apykaita. Glikolizės ... metu  $C_6H_{12}O_6$  virsta  $CO_2$  arba jos anglies atomas iš  $\beta$  pozicijos nukeliauja iki  $CH_3$

Poliaininai suaktyvina „DNR raišką“



# VIENANGLIŲ FRAGMENTŲ APYKAITOS SCHEMA



# Matematikai modeliuoja biologinius- molekulinius procesus

1. Glikolizės matematinis modeliavimas

<https://www.nature.com/articles/s41598-018-20348-7>

<https://www.nature.com/articles/s41598-019-39901-z>

2. Oksidacinio fosforilinimo (tolesnio energijos gaminimo ATF pavidale) modeliavimas

<https://www.mdpi.com/2073-4409/11/24/4020>

4. Vienanglių fragmentų, apjungiant glikolizės procesą modeliavimas

<https://academic.oup.com/jn/article/136/10/2653/4746711>

Mathematical Models of Folate-Mediated One-Carbon Metabolism H. F. Nijhout,\* M. C. Reed,† and C. M. Ulrich <https://sites.duke.edu/metabolism/files/2015/11/08litwack.pdf>

5. Metionino ciklo matematinis modeliavimas

[https://www.researchgate.net/publication/8991844\\_A\\_Mathematical\\_model\\_of\\_the\\_methionine\\_cycle](https://www.researchgate.net/publication/8991844_A_Mathematical_model_of_the_methionine_cycle)

6. Poliaminų sintezės matematinis modeliavimas

[https://www.researchgate.net/publication/7071327\\_Mathematical\\_Modeling\\_of\\_Polyamine\\_Metabolism\\_in\\_Mammals](https://www.researchgate.net/publication/7071327_Mathematical_Modeling_of_Polyamine_Metabolism_in_Mammals)

8. Imuninės sistemos matematinis modeliavimas

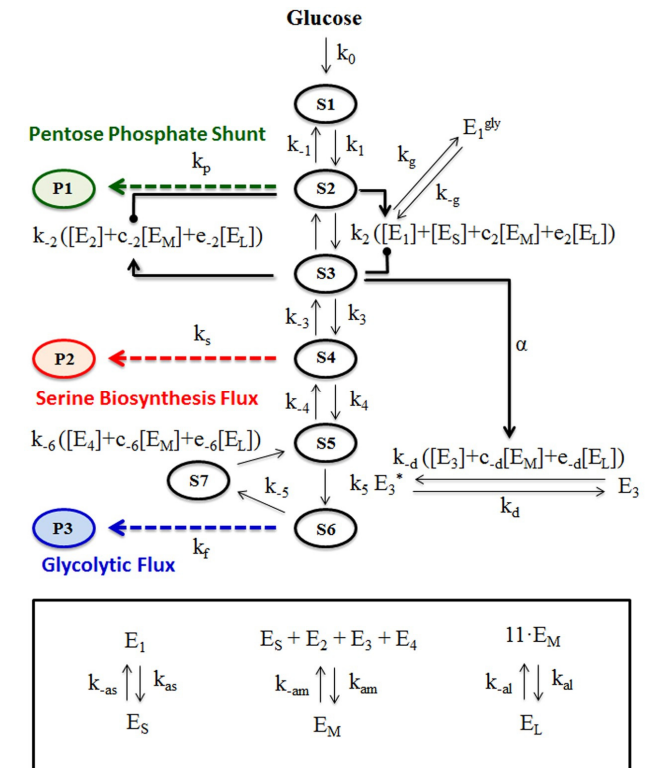
<https://www.ncbi.nlm.nih.gov/pmc/articles/PMC6579737/>

9. Biocheminių tinklų matematinis modeliavimas [Effect of substrate competition in kinetic models of metabolic networks – ScienceDirect https://ars.els-cdn.com/content/image/1-s2.0-S0014579313004833-mmc1.pdf](https://ars.els-cdn.com/content/image/1-s2.0-S0014579313004833-mmc1.pdf)

Matematiniai modeliai: tarp įmanomų modelinių uždavinių ir tarp tų, kuriuos reikia spręsti - atskiri reakcijų tinklo fragmentai

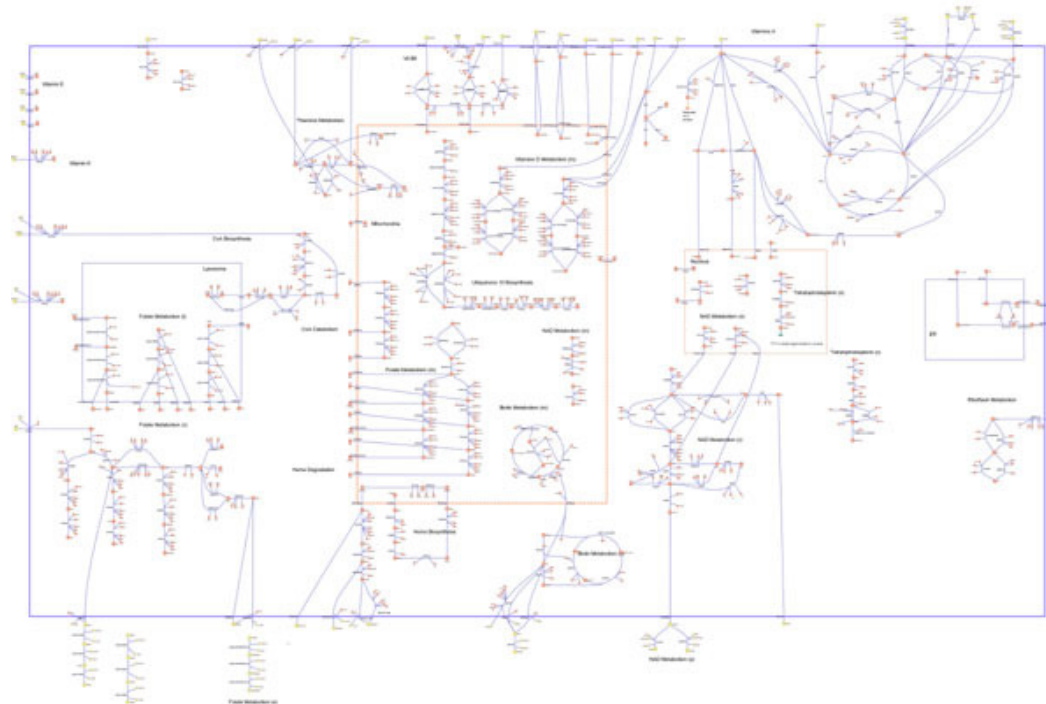
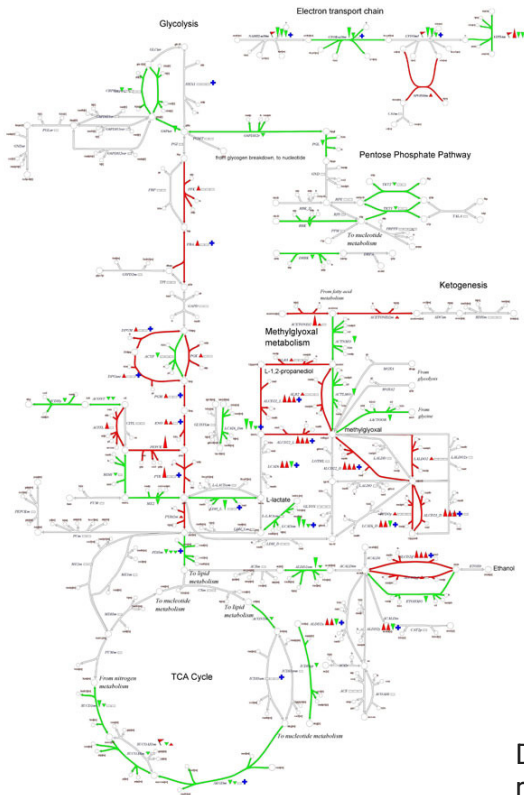
$$\begin{aligned}
 dA(t)/d(t) &= k_{AAex} - V_f A(t) / (K_m A + A(t)) \\
 dA_1(t)/d(t) &= V_f A(t) / (K_m A + A(t)) - V_f A_1(t) / (K_m A + A_1(t)) \\
 dA_2(t)/d(t) &= V_f A_1(t) / (K_m A + A_1(t)) - V_f A_2(t) / (K_m A + A_2(t)) \\
 dB(t)/d(t) &= k_{BBex} - V_f B(t) / (K_m B + B(t)) \\
 dB_1(t)/d(t) &= V_f B(t) / (K_m B + B(t)) - V_f B_1(t) / (K_m B + B_1(t)) \\
 dB_2(t)/d(t) &= V_f B_1(t) / (K_m B + B_1(t)) - V_f B_2(t) / (K_m B + B_2(t))
 \end{aligned}$$

[1-s2.0-S0014579313004833-mmc1.pdf](#)



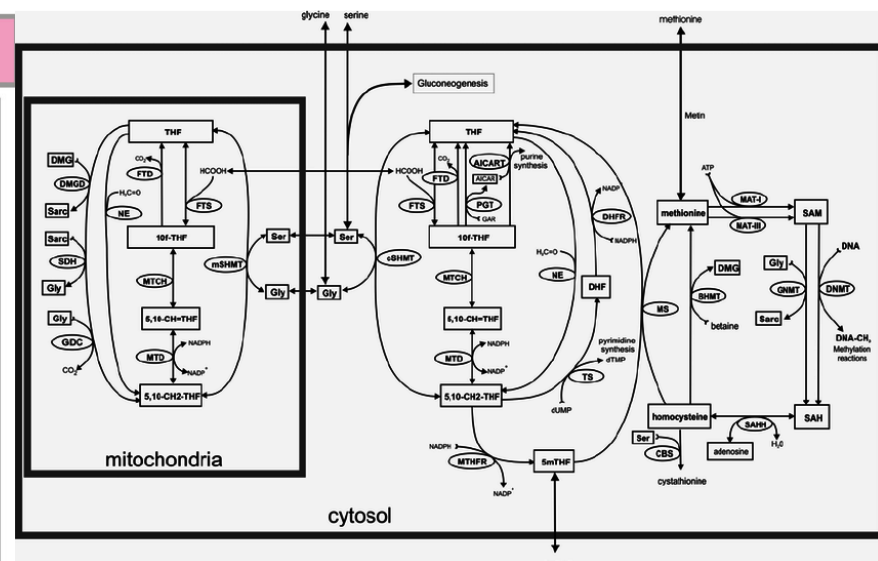
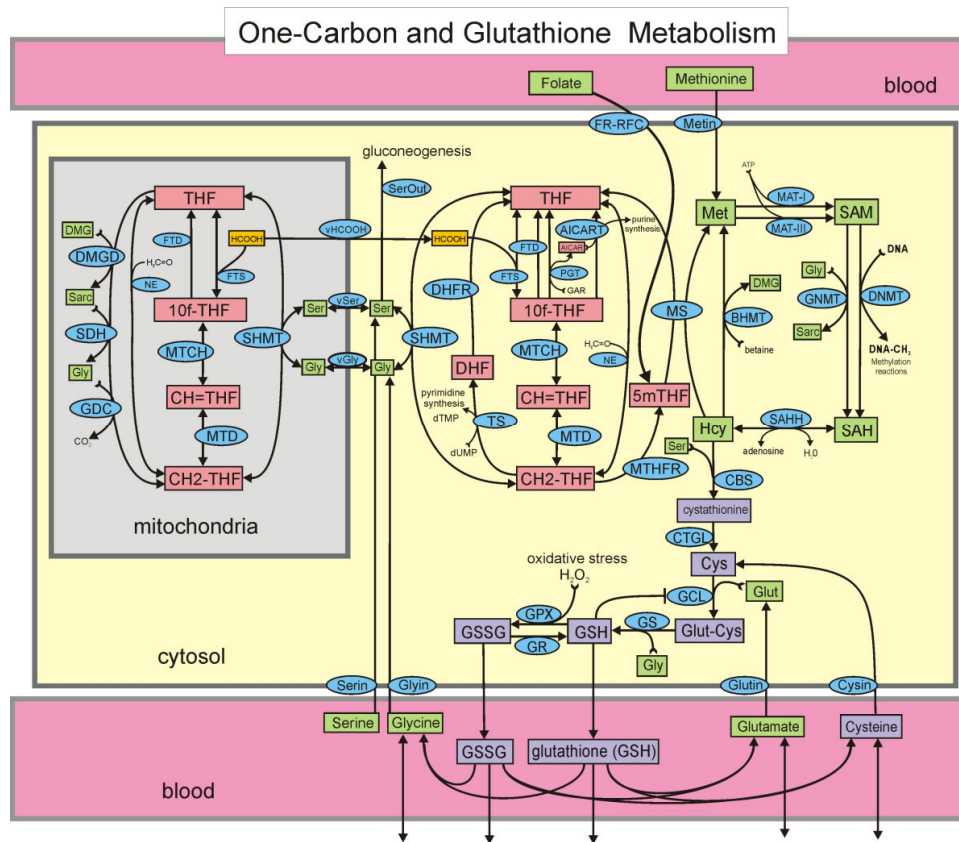
# Balanso modelis (Recon1, Recon2)

## Homo sapiens Recon 1 VITAMIN & COFACTOR METABOLISM



Duarte NC, Becker SA, Jamshidi N, Thiele I, Mo ML, Vo TD, Srivas R, Palsson BØ. Global reconstruction of the human metabolic network based on genomic and bibliomic data. Proc Natl Acad Sci U S A. 2007 Feb 6;104(6):1777-82. doi: 10.1073/pnas.0610772104. Epub 2007 Jan 31.

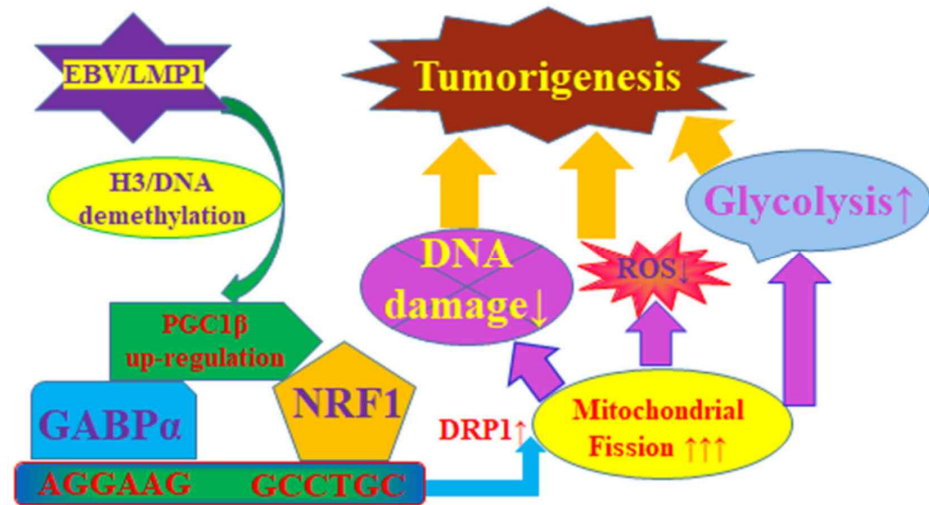
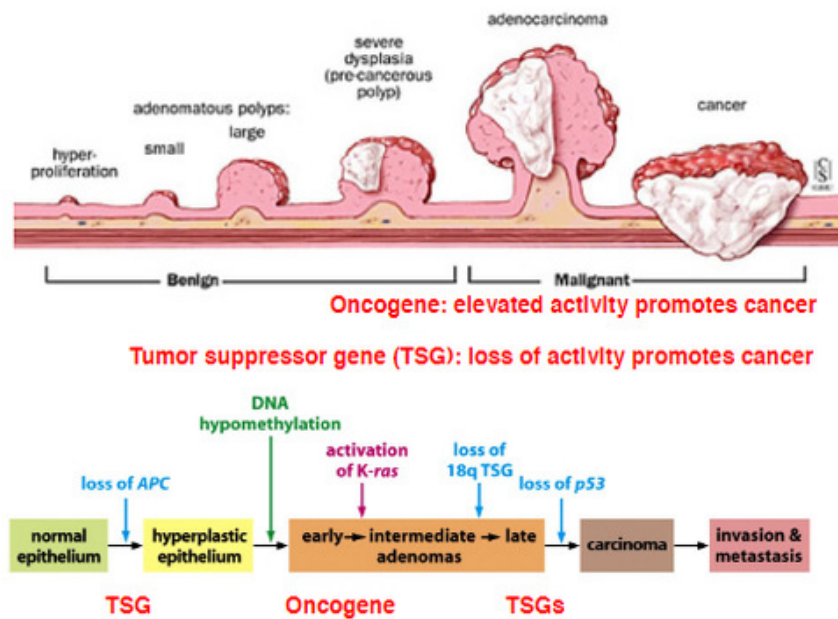
## 1C apykaitos modeliavimas folatų, metionino ciklo ir radikalų eliminavimo schemeje



2004-2008 metų modeliai: Nijhout... Reed et al. (2007)

„Įdomu tai, kad vienanglių fragmentų metabolizmo genai *SHMT2* ir *MTHFD2*, koduojantys mitochondrijų serino hidrometiltransferazę ir metilen-tetrahydrofolato dehidrogenazę / ciklohidrolazę, buvo nustatyti tarp 50 dažniausiai didžiausios raiškos genų“

# II dalis. TUMORIGENEZĖS MODELIS



# Trys vėžio aprašo terminijos lygmenys

- KLINIKINIS (TNM klasifikacija)
- BIOLOGINIS
- MOLEKULINIS-ELEMENTARIŲJŲ DALELIŲ

## Būtinės ir pakankamos naviko aprašo sąlygos:

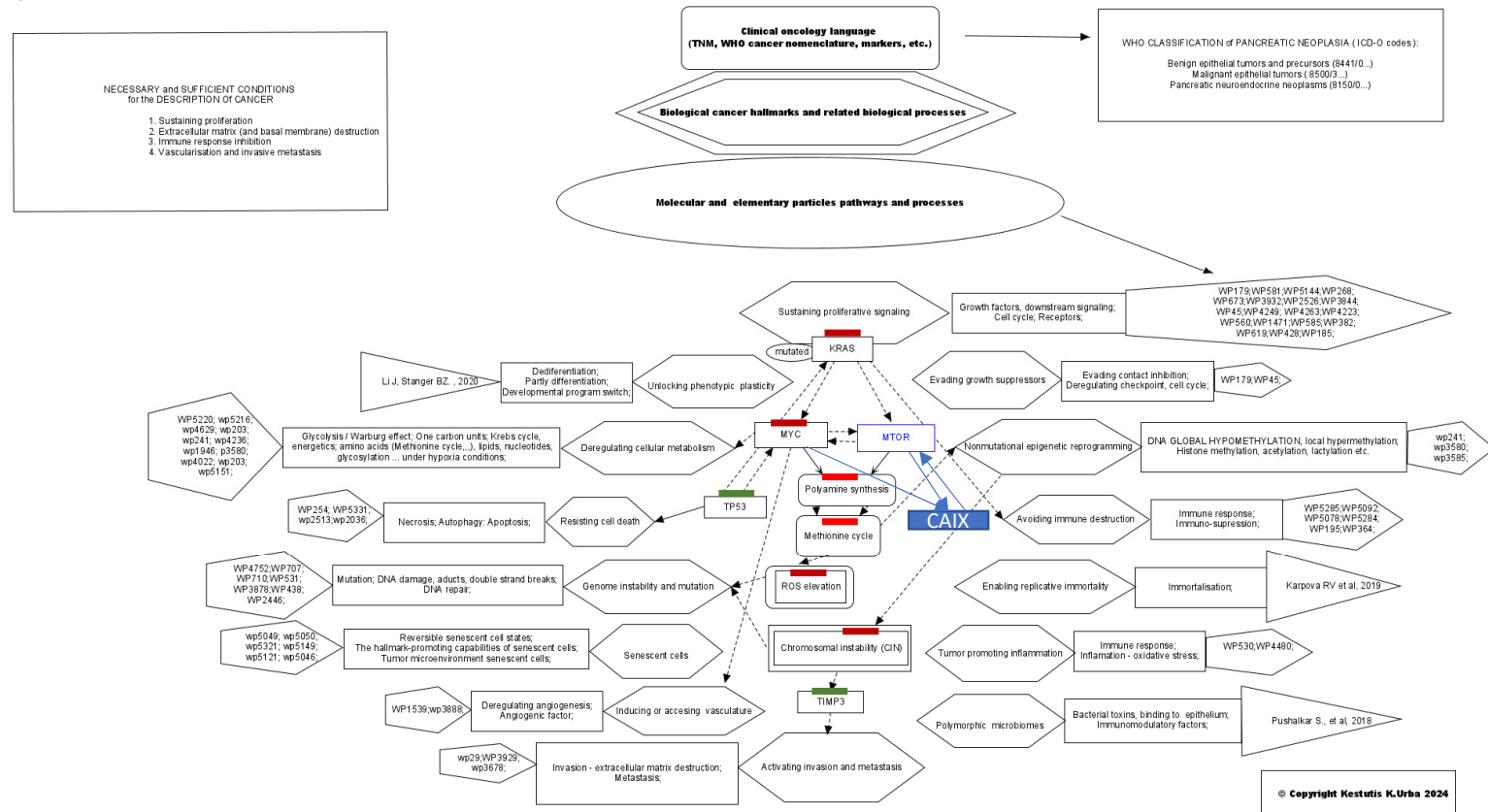
- I. Spartesnė piktybinių ląstelių sankaupos proliferacija nei aplinkinio audinio
- II. Tarpląstelinių jungčių, bazalinės membranos ir ekstraceliulinio matriksio griovimas bei ardymas
- III. Naviko angiogenezė-kapiliarizacija ir metastazavimas
- IV. Imuninio atsako slopinimas



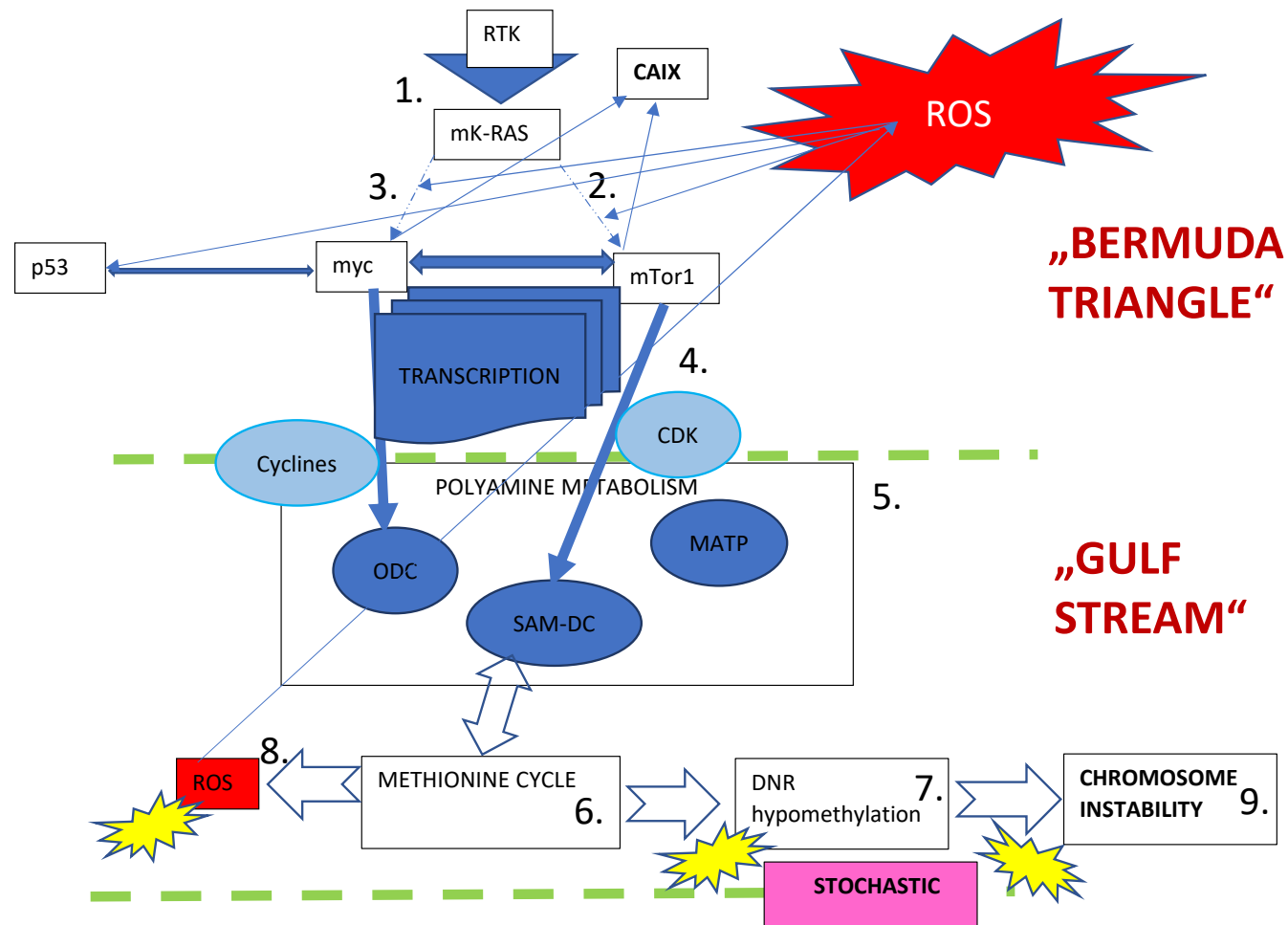
*Hanahan-Weinberg 2000, 2011, 2022,  
([Baker S, Ali I, Silins I, et al. 2017](#))*

# Molekulinio ir biologinio lygmenų sąryšis vėžio apraše

Title: Three levels of cancer description 14  
Organism: Homo sapiens



CELL “undruggable” mK-ras INVOLVED CARCINOGENESIS and MALIGNIZATION SCENARIO (K.Urba, 2022, © copyright)

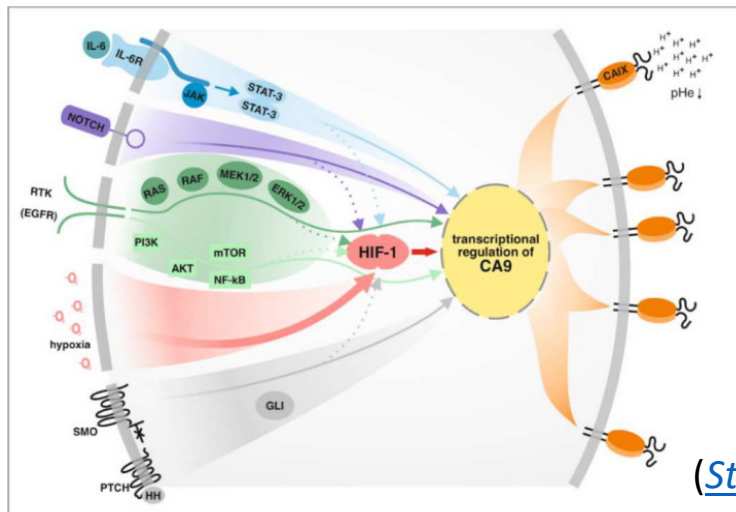


mK-ras is not only „driver“ but long distance long time stochastic „trigger“ too!

Stochasticity: 

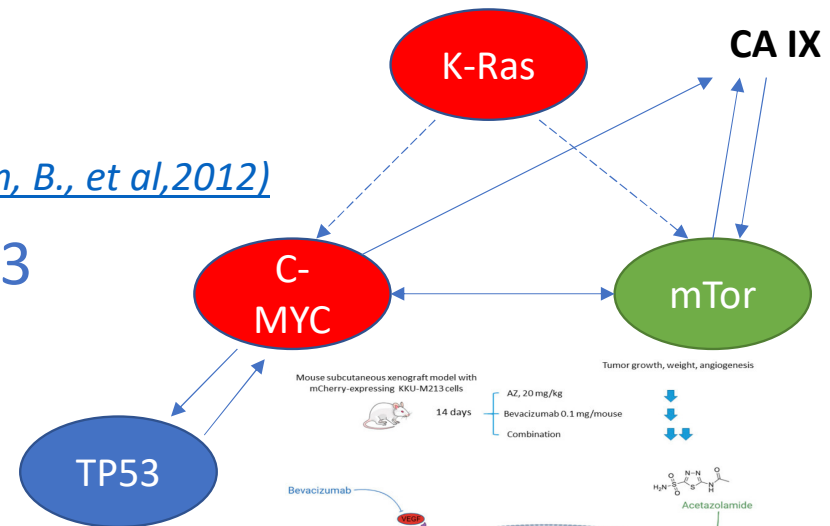
# Keletas onkogenų, augimo veiksnių, supresorių

- Onkogenas **K-ras**
- Onkogenas **C-myc**
- Onkogenų slopiklis (supresorius) **TP53**
- Augimo faktorius kompleksas **mTor**

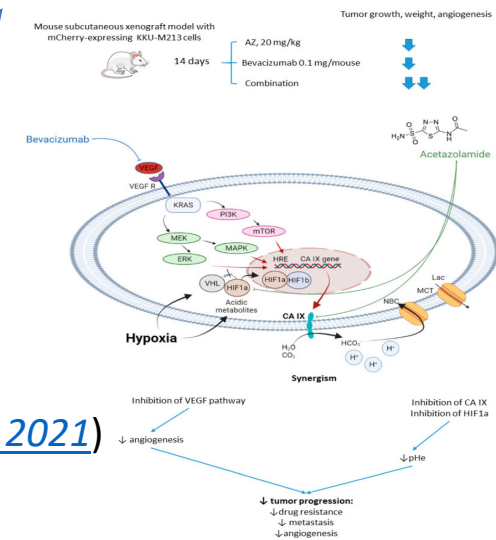


(Strapcova S., et al, 2020)

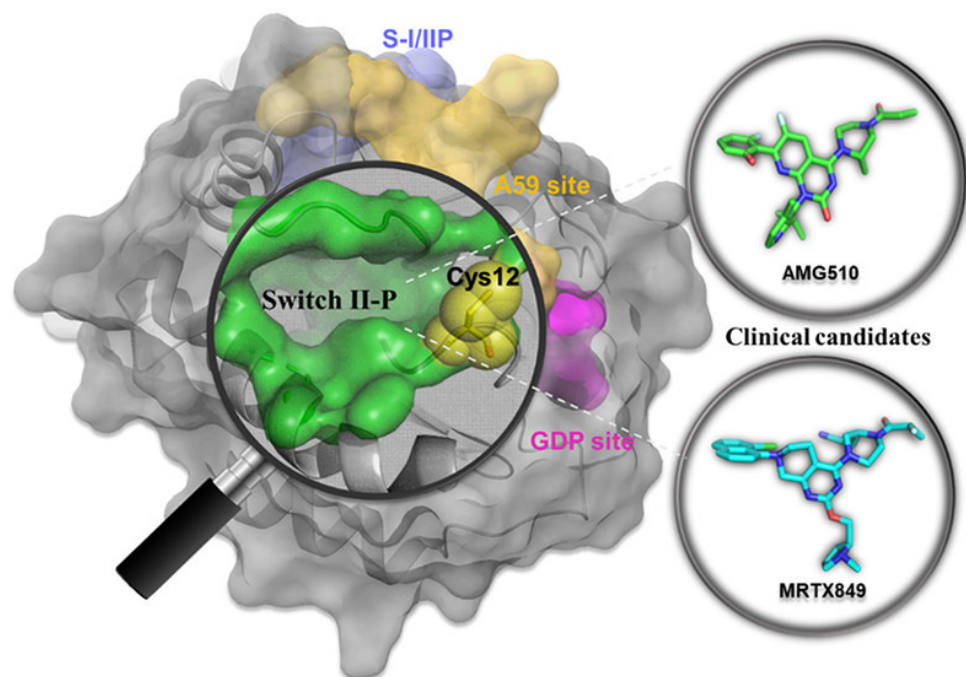
(Kim, B., et al, 2012)



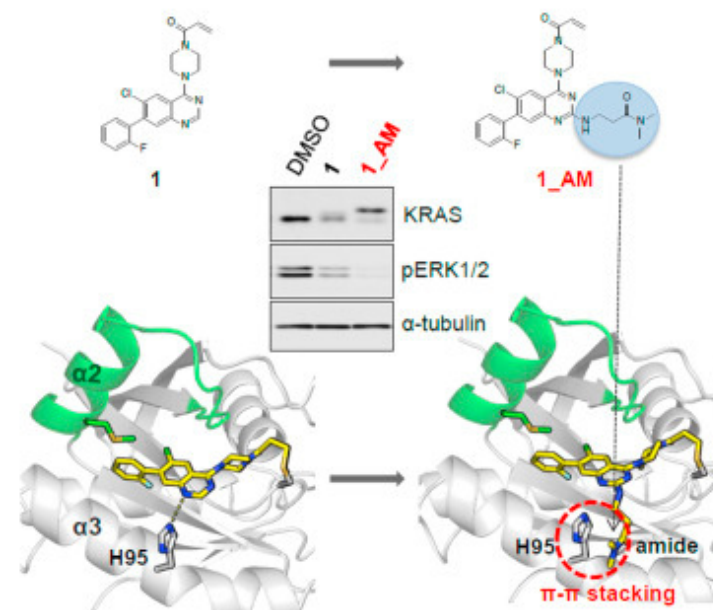
(Kalinin S., et al, 2021)



# Tiesioginis K-RAS slopinimas



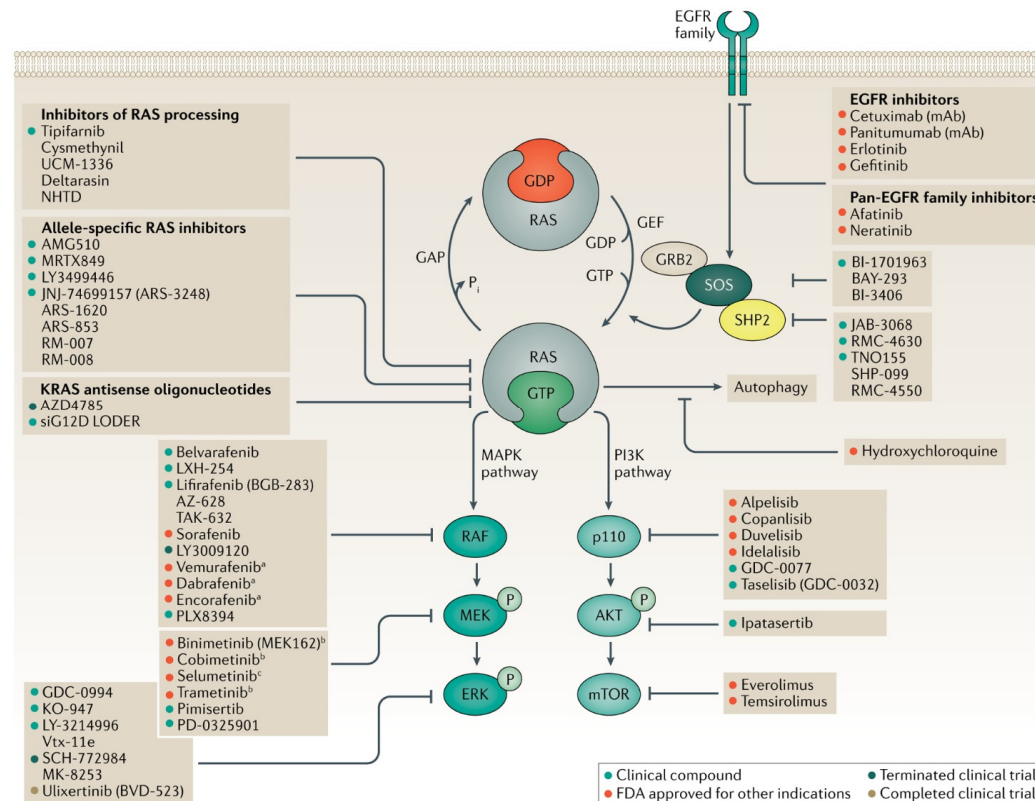
Developing more potent and selective inhibitors for KRAS G12C



Olivier T, Haslam A, Prasad V. **Sotorasib in KRAS<sup>G12C</sup> mutated lung cancer: Can we rule out cracking KRAS led to worse overall survival?** Transl Oncol. 2023 Feb;28:101591. doi: 10.1016/j.tranon.2022.101591. Epub 2022 Dec 26. PMID: 36577165; PMCID: PMC9803768.

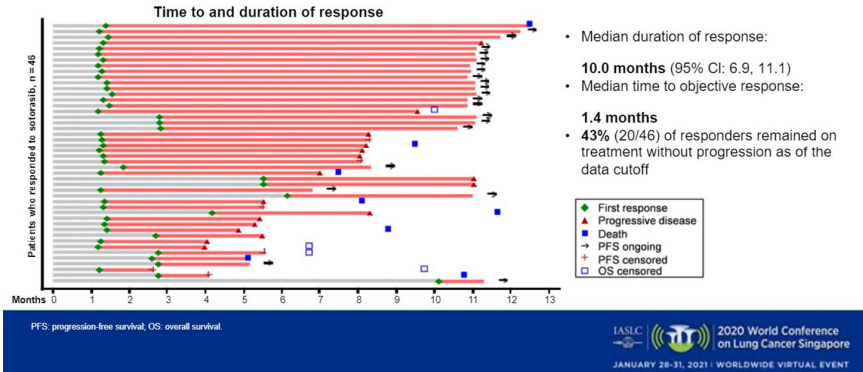
# RAS-targeted therapies: is the undruggable drugged?

[Amanda R. Moore](#), [Scott C. Rosenberg](#), [Frank McCormick](#), [Shiva Malek](#), Nat Rev., 2020



## Durability of Tumor Response

Responses to sotorasib were durable; 72% were seen at the first assessment



## Sotorasib Shows Early Activity Against KRAS G12C Mutant NSCLC



**Chris Evelo** is the founder and head of the department of Bioinformatics - BiGCaT at Maastricht University; WikiPathways



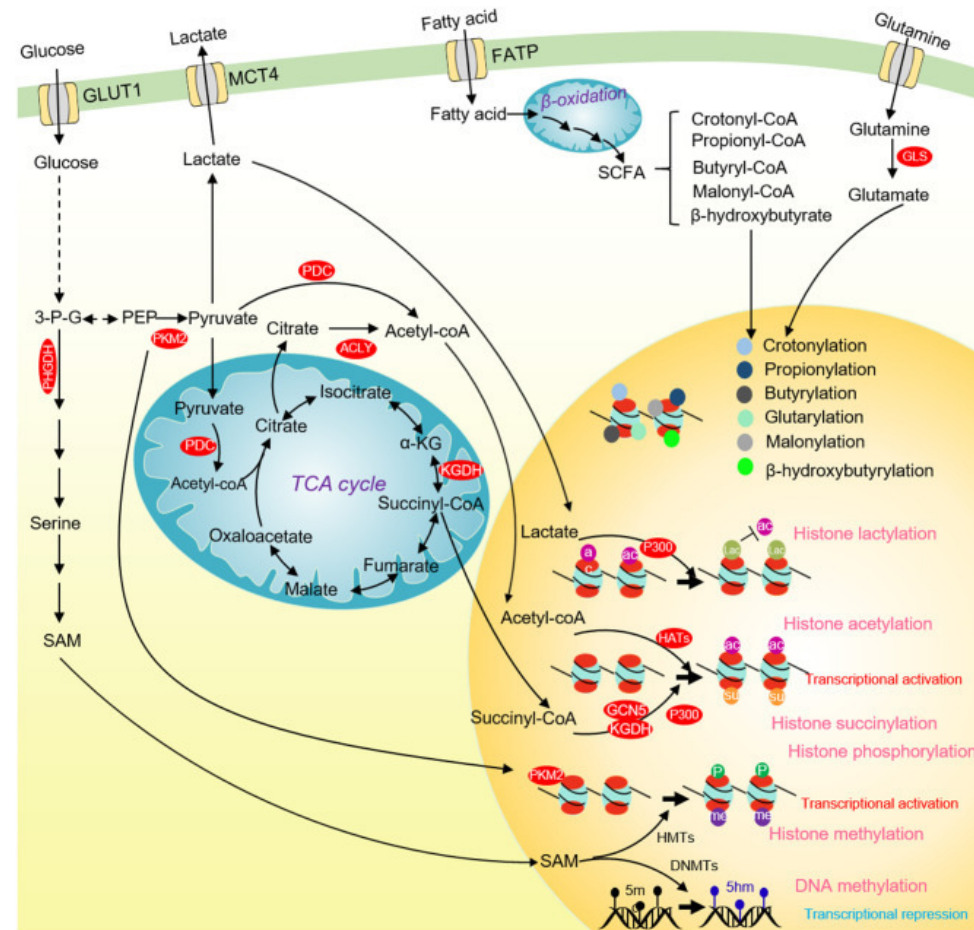
Dear Kestutis,

thank you for your thoughtful email. I agree that targeting MYC as a major downstream effector of KRAS is likely to be effective, as predicted from **mouse models** using inducible RAS and MYC systems. I had not given much thought to the possibility of targeting polyamines and/or ODC, though my PhD thesis focused on regulation of ODC during viral infections. I appreciate your comments and will give these matters more attention.

With best regards  
Frank

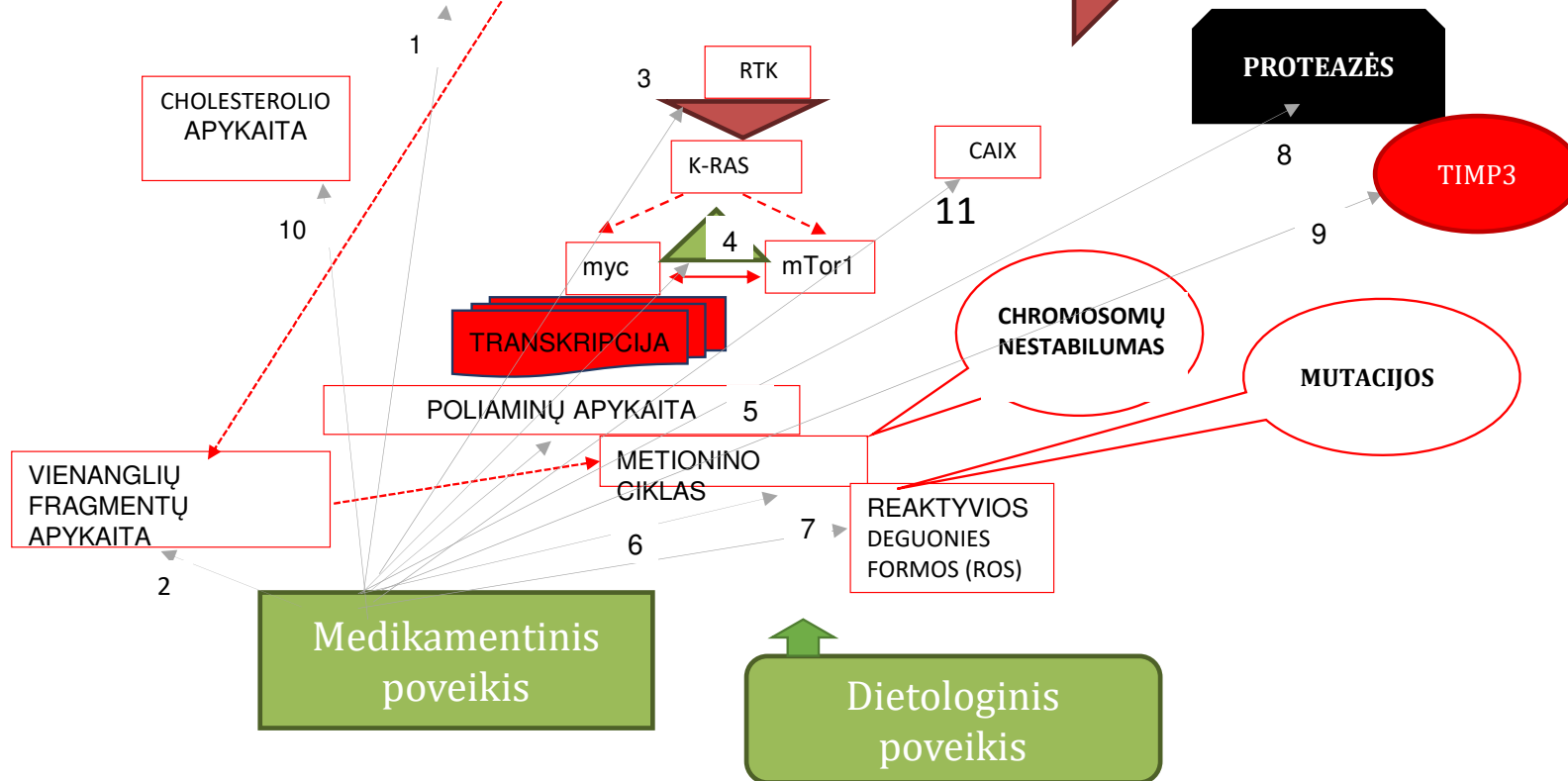
Frank McCormick, PhD, FRS,  
UCSF Helen Diller Family Comprehensive Cancer Center,  
Room HD-371  
1450 3rd Street,  
San Francisco, CA 94158-9001  
415 218 0155 (Cell phone)

Ma R, Wu Y, Li S, Yu X. **Interplay Between Glucose Metabolism and Chromatin Modifications in Cancer.** Front Cell Dev Biol. 2021 Apr 27;9:654337. doi: 10.3389/fcell.2021.654337. PMID: 33987181; PMCID: PMC8110832



# Vienuolika adaptyvios kompleksinės medikamentinės terapijos schemas krypčių

Glikolizė: ATF ir aktyvinantis transkripciją laktilimas



# Dinaminių sistemų onkologijoje modeliavimas

- Penkių tipų dinaminiai modeliai pagal apžvalgą [Markert EK, Vazquez A. Mathematical models of cancer metabolism. Cancer Metab. 2015;3:14.](#)

[Published 2015 Dec 22. doi:10.1186/s40170-015-0140-6:](#)

- Genų biologinės raiškos (Proliferacija/audinio Remodeliavimas: „P–/R–, P–/R+, P+/R– ir P+/R+“)
- Srautų balanso (stacionarumas: „metabolitų koncentracija ir biocheminių reakcijų greitis laikui bėgant išlieka pastovūs“) -tik vidurkinės charakteristikos dėl plačių pasikliautinių intervalų riboja prognozių tikslumą, 2007 m.
- Srautų kinetiniai („Pagrindiniai veiksniai yra fermento apykaitos greitis, fermento koncentracija, substrato prisotinimo terminas ir termodinamikos terminas, susijęs su fermento savybėmis esant pusiausvyrai“ – gerėja prognozė) 2012-2014 m.
- Difuziniai (jonų, molekulių pernešimo per membranas modeliai su fizikinėmis savybėmis)
- Mechaniniai („Pagrindinis iššūkis - nustatyti ryšius tarp ląstelės charakterizuojančių savybių ir ląstelių-ląstelių sąveikos su naviko mechaninėmis savybėmis“, elastingumas)

# Matematinis chemo-imunoterapijos modelis

Nave O. A [mathematical model for treatment using chemo-immunotherapy](#). Heliyon. 2022 Apr 26;8(4):e09288. doi: 10.1016/j.heliyon.2022.e09288. PMID: 35520602; PMCID: PMC9065634.

„Let  $\vec{U}$  be the vector of the dynamic variables of the system:  $\vec{U} = (D_I, D, D_T, T_N, T_C, T_{CP}, T_R, IL_2, IL_{10}, C, C_H)$ .

The analytical function  $F$  describes chemotherapy treatment, which is a combination of chemotherapy and immunotherapy. The function depends on time  $t$  and dosage  $q$ .

The function has the form:

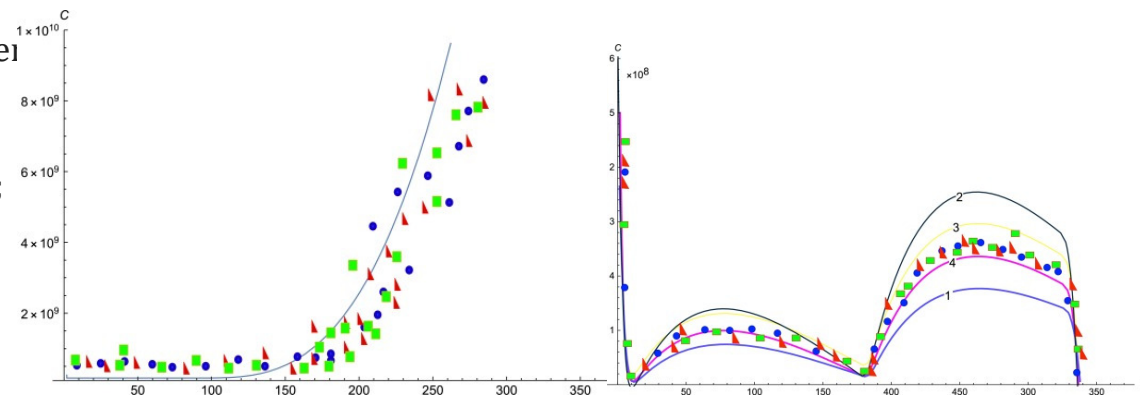
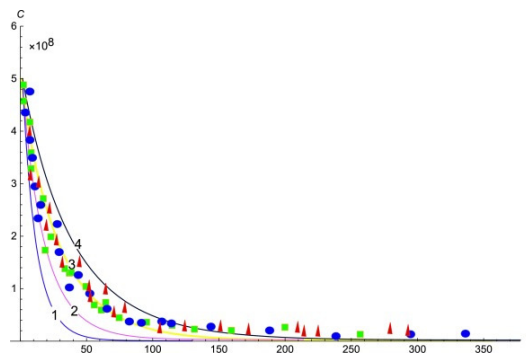
$$F(q, t) = \sum q(t - mk)H(t - mk)e_{t - mk/0.5}$$

The model (11 netiesinių lygčių) can be written in abbreviated form as

$$d\vec{U}/dt = \vec{F}(\vec{U}), \quad \vec{U}(0) = \vec{U}_0,$$

where  $\vec{F}(\vec{U})$  is the vector field of the model;

that is,  $\vec{F}(\vec{U}) = (F_1(\vec{U}), \dots, F_{11}(\vec{U}))$



Smegenų auglio ląstelių dinamika be gydymo ir su gydymu kas 28 d. ir kas 7 d.



# Kompleksinis TUMORIGENEZĖS matematinis modelis Nr.1 turi susidėti iš:

RTK – K-ras, MAPK, PI3K, tp 53 sąveikos bloko

Erickson KE, Rukhlenko OS, Posner RG, Hlavacek WS, Kholodenko BN. New insights into RAS biology reinvigorate interest in **mathematical modeling** of RAS signaling. Semin Cancer Biol. 2019 Feb;54:162-173  
Sulaimanov N, Klose M, Busch H, Boerries M. Understanding the mTOR signaling pathway via **mathematical modeling**. Wiley Interdiscip Rev Syst Biol Med. 2017 Jul;9(4):e1379. doi: 10.1002/wsbm.1379. Epub 2017 Feb 10. PMID: 28186392; PMCID: PMC5573916.

Poliaminų apykaitos modelio

Rodríguez-Caso C, Montañez R, Cascante M, Sánchez-Jiménez F, Medina MA. **Mathematical modeling** of polyamine metabolism in mammals. J Biol Chem. 2006 Aug 4;281(31):21799-21812. doi: 10.1074/jbc.M602756200. Epub 2006 May 18. PMID: 16709566.

Bao K, Liang G, Tian T, Zhang X. Mathematical modeling of combined therapies for treating tumor drug resistance. Math Biosci. 2024 May;371:109170. doi: 10.1016/j.mbs.2024.109170. Epub 2024 Mar 11. PMID: 38467302.

Chen T, Ali Al-Radhawi M, Sontag ED. **A mathematical model** exhibiting the effect of DNA methylation on the stability boundary in cell-fate networks. Epigenetics. 2021 Apr;16(4):436-457.

Glikolizės, Serino sintezės Folato – B12, B6, Metionino ciklo modelio (1c apykaita)

Saa PA, Nielsen LK. Construction of feasible and accurate kinetic models of metabolism: **A Bayesian approach**. Sci Rep. 2016 Jul 15;6:29635. doi: 10.1038/srep29635. PMID: 27417285; PMCID: PMC4945864

Kompleksinės vaistinės terapijos

Pereira EJ, Smolko CM, Janes KA. **Computational Models** of Reactive Oxygen Species as Metabolic Byproducts and Signal-Transduction Modulators. Front Pharmacol. 2016 Nov 29;7:457. doi: 10.3389/fphar.2016.00457. PMID: 27965578; PMCID: PMC5126069

Radikalų eliminavimo – ROS sistemoje GSH

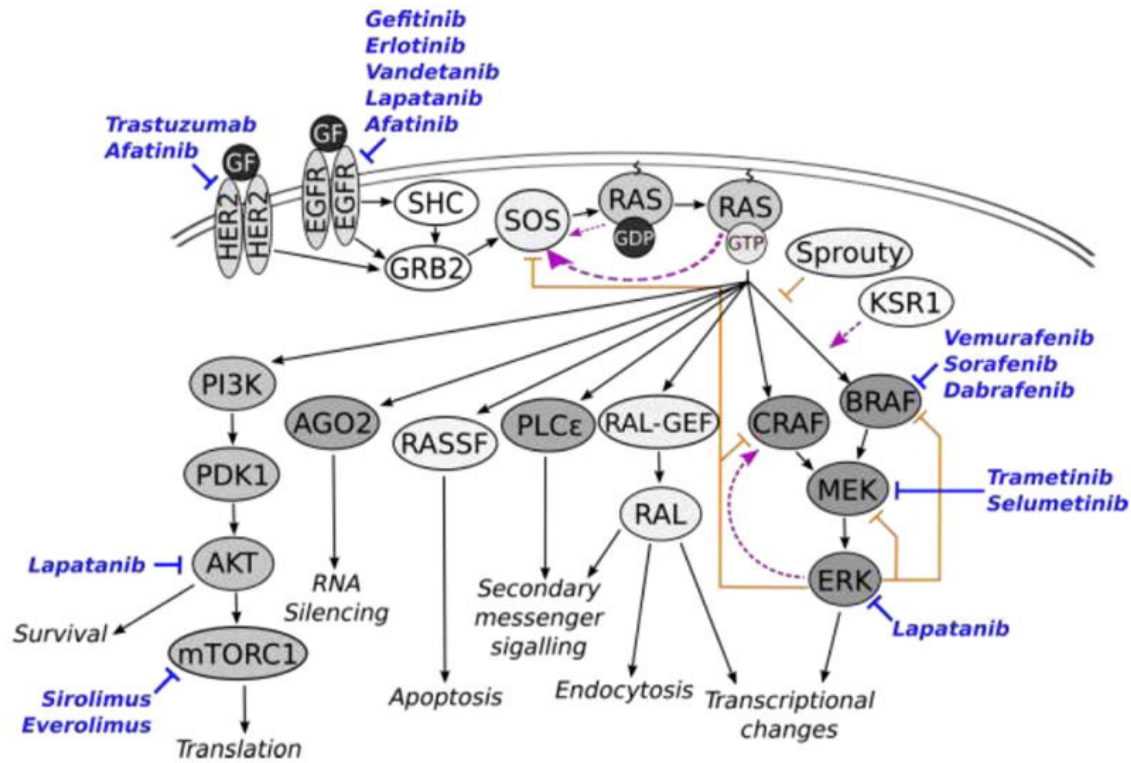
Lynch AR, Arp NL, Zhou AS, Weaver BA, Burkard ME. Quantifying chromosomal instability from intratumoral karyotype diversity using agent-based **modeling and Bayesian inference**. Elife. 2022 Apr 5;11:e69799. doi: 10.7554/eLife.69799. PMID: 35380536; PMCID: PMC9054132.

Genominio – chromosominio nestabilumo

Ekstraceliulinio matrikso ardymo ir angiogenezės

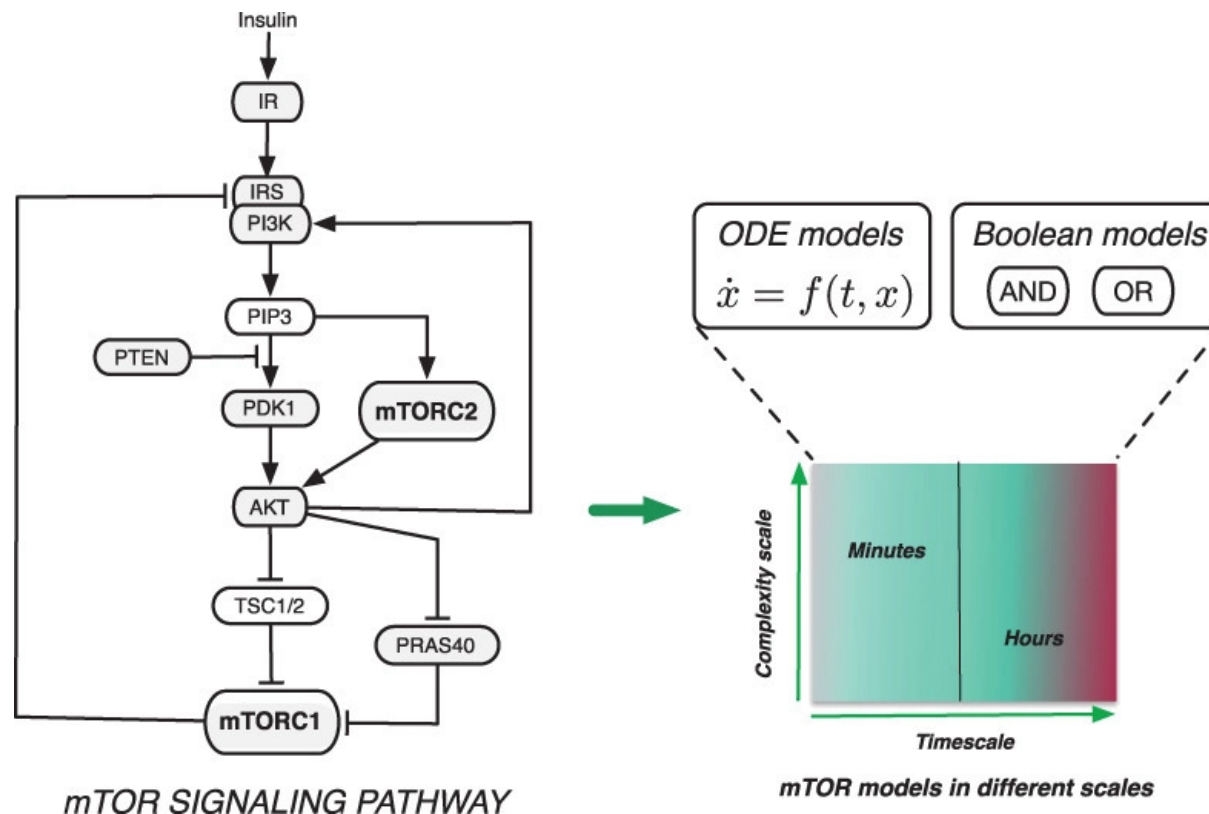
Imuninės terapijos

1. Erickson KE, Rukhlenko OS, Posner RG, Hlavacek WS, Kholodenko BN. New insights into RAS biology reinvigorate interest in **mathematical modeling** of RAS signaling. Semin Cancer Biol. 2019 Feb;54:162-173



|          | $k_a$<br>GTP (1/<br>M/s) | $k_{d,GTP}$ (1<br>/s) | $k_{3,GDP}$ (1<br>/M/s) | $k_{d,GDP}$ (1<br>/s) | $k_{hyd}$ (1/s) |         |         |         |         |       |
|----------|--------------------------|-----------------------|-------------------------|-----------------------|-----------------|---------|---------|---------|---------|-------|
|          | None<br>(WT)             |                       |                         | 2.05E-4               | [37]            |         | 6.33E-5 | [48]    | 1.47E-4 |       |
| RAS      |                          |                       | 1.00E-4                 | [174]                 |                 |         | 4.20E-4 | [174]   | 3.40E-4 | [174] |
| Mutation |                          |                       | 2.00E-3                 | [175]                 |                 |         | 2.00E-3 | [175]   | 6.80E-4 | [175] |
| n        | 1.40E8                   | [174]                 | 9.00E-5                 | [176]                 | 5.10E7          | [174]   | 1.20E-4 | [176]   | 2.10E-4 | [176] |
|          | 2.20E6                   | [173]                 | 2.50E-4                 | [177]                 | 2.30E6          | [173]   | 1.08E-4 | [177]   | 3.49E-4 | [177] |
|          |                          |                       | 2.33E-4                 | [180]                 |                 |         | 3.00E-5 | [38]    | 9.30E-3 | [38]  |
|          |                          |                       |                         |                       |                 |         | 2.17E-4 | [180]   | 2.17E-4 | [180] |
|          |                          |                       |                         |                       |                 |         | 1.60E-5 | [173]   |         |       |
|          |                          |                       |                         |                       |                 |         |         |         |         |       |
| G12A     |                          |                       |                         | 200E-3                | [175]           |         | 2.00E-3 | [175]   | 1.30E-5 |       |
|          |                          |                       |                         |                       |                 |         |         |         |         |       |
| G12C     |                          |                       |                         | 2.00E-3               | [175]           |         | 2.00E-3 | [175]   | 4.90E-4 |       |
|          |                          |                       |                         |                       |                 |         |         |         |         |       |
| G12D     |                          |                       |                         | 5.00E-4               | [174]           |         | 2.00E-4 | [174]   | 1.50E-4 |       |
|          |                          |                       | 2.00E-3                 | [175]                 |                 |         | 2.00E-3 | [175]   | 1.90E-4 | [175] |
| 4.80E8   | [174]                    | 9.50E-4               | [176]                   | 7.00E7                | [174]           | 1.60E-4 | [176]   | 1.40E-4 | [176]   |       |
| 7.54E6   | [30]                     | 1.25E-3               | [30]                    | 3.16E6                | [30]            | 5.16E-5 | [30]    | 1.40E-4 | [30]    |       |
|          |                          |                       |                         |                       |                 |         |         |         |         |       |
|          |                          |                       |                         |                       |                 |         |         |         |         |       |
| G12E     |                          |                       |                         |                       |                 |         |         |         |         |       |
|          |                          |                       |                         |                       |                 |         |         |         |         |       |
| G12R     |                          |                       |                         | 2.00E-3               | [175]           |         | 2.00E-3 | [175]   | 1.80E-5 |       |
|          |                          |                       |                         |                       |                 | 6.17E-3 | [181]   |         |         |       |

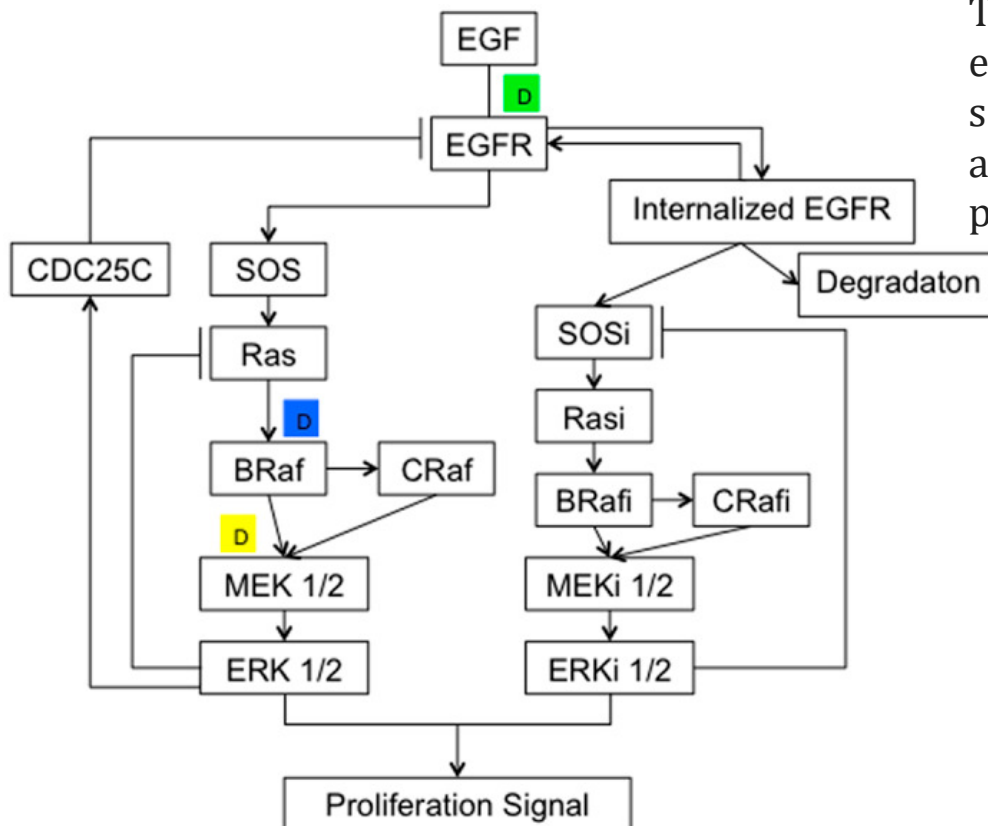
2. Sulaimanov N, Klose M, Busch H, Boerries M. Understanding the mTOR signaling pathway via **mathematical modeling**. Wiley Interdiscip Rev Syst Biol Med. 2017 Jul;9(4):e1379. doi: 10.1002/wsbm.1379. Epub 2017 Feb 10. PMID: 28186392; PMCID: PMC5573916.



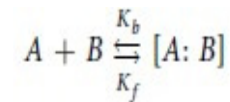
23 publikacijos, pradedant 2002 m. iki 2017 m., skirtos mTor kelio matematiniam modeliavimui. Po to dar 19 citavimų...

| mTOR Models                              | Biological Context                                            | Model Type     | Model Size | Timescale |
|------------------------------------------|---------------------------------------------------------------|----------------|------------|-----------|
| Dalle Pezze et al. <a href="#">43</a>    | Mechanisms of mTORC2 regulation                               | ODE            | 25–33      | 0–120 min |
| Sontag et al. <a href="#">44</a>         | mTOR-AMPK crosstalk                                           | ODE            | 26–28      | 0–120 min |
| Kubota et al. <a href="#">45</a>         | Decoding insulin signal in the mTOR pathway                   | ODE            | 11         | 0–600 min |
| Toyoshima et al. <a href="#">46</a>      | Signal transfer in the mTOR pathway                           | ODE            | 3–4        | 0–120 min |
| Noguchi et al. <a href="#">47</a>        | Metabolism regulation by the mTOR pathway                     | ODE            | 15         | 0–480 min |
| Borisov et al. <a href="#">48</a>        | MAPK-mTOR crosstalk                                           | ODE            | 78         | 0–30 min  |
| Fujita et al. <a href="#">49</a>         | Signal transfer in the mTOR pathway                           | ODE            | 3–8        | 0–120 min |
| Jain et al. <a href="#">50</a>           | BDNF-mTOR crosstalk                                           | ODE            | 130        | 0–30 min  |
| Wu et al. <a href="#">51</a>             | mTOR-MAPK-PKC crosstalk                                       | Boolean        | 19–22      | 0–60 min  |
| Hatakeyama et al. <a href="#">52</a>     | mTOR-MAPK crosstalk                                           | ODE            | 33–34      | 0–30 min  |
| Sedaghat et al. <a href="#">53</a>       | Metabolic insulin signaling                                   | ODE            | 21         | 0–60 min  |
| Faratian et al. <a href="#">54</a>       | mTOR-MAPK crosstalk                                           | ODE            | 56         | 0–60 min  |
| Brännmark et al. <a href="#">55</a>      | Mechanisms of receptor internalization                        | ODE            | 5          | 0–30 min  |
| Brännmark et al. <a href="#">56</a>      | Mechanisms of insulin resistance                              | ODE            | 26–27      | 0–30 min  |
| Vinod et al. <a href="#">57</a>          | mTOR regulation via amino acids                               | ODE            | 10–13      | 0–30 min  |
| Araujo et al. <a href="#">58</a>         | Feedback characterization in the mTOR pathway                 | ODE            | 4–5        | a.u.      |
| Giri et al. <a href="#">59</a>           | Input–output characterization in metabolic insulin signaling  | Algebraic      | 22         | a.u.      |
| Tian and Wu <a href="#">60</a>           | Robustness property of the mTOR pathway                       | ODE            | 16         | a.u.      |
| Wang and Krueger <a href="#">61</a>      | Bifurcation analysis of the mTOR pathway                      | Algebraic      | 2          | a.u.      |
| Nguyen and Kholodenko <a href="#">62</a> | Feedback regulation in the mTOR-MAPK pathways                 | ODE            | 29         | a.u.      |
| Kriete et al. <a href="#">63</a>         | Metabolism regulation by the mTOR and NF- $\kappa$ B pathways | Fuzzy-logic    | 34         | a.u.      |
| Mosca et al. <a href="#">64</a>          | Metabolism regulation by the mTOR pathway                     | ODE, Algebraic | 25         | a.u.      |

3. Huang L, Jiang Y, Chen Y. Predicting Drug Combination Index and Simulating the Network-Regulation Dynamics by **Mathematical Modeling** of Drug-Targeted **EGFR-ERK** Signaling Pathway. Sci Rep. 2017 Jan 19;7:40752. doi: 10.1038/srep40752. PMID: 28102344;



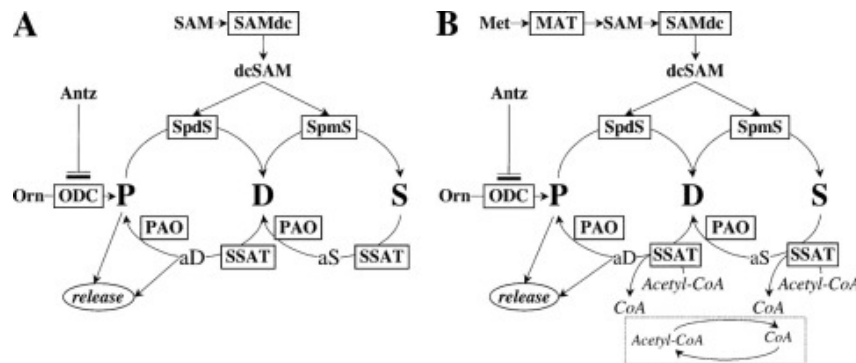
The model contains 126 distinct molecular species, and 190 elementary reactions; these reactions are described as a series of ordinary differential equations based on the mass action law. The model is parameterized by 123 kinetic parameters and 126 initial molecular concentrations.



$$\frac{dA}{dt} = K_b \cdot [A: B] - K_f \cdot A \cdot B$$

(1)

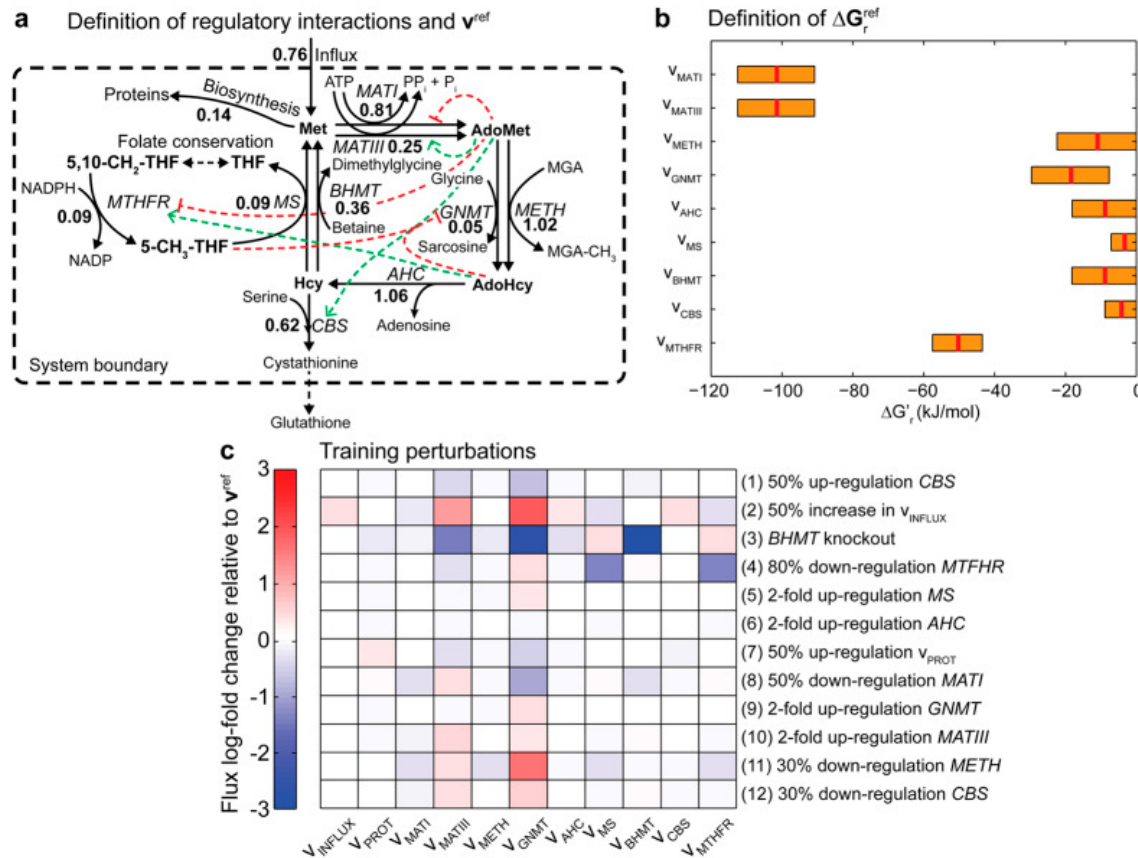
# 4. Poliaminų modeliavimas



5. Rodríguez-Caso C, Montañez R, Cascante M, Sánchez-Jiménez F, Medina MA. **Mathematical modeling** of polyamine metabolism in mammals. J Biol Chem. 2006 Aug 4;281(31):21799-21812. doi: 10.1074/jbc.M602756200. Epub 2006 May 18. PMID: 16709566.

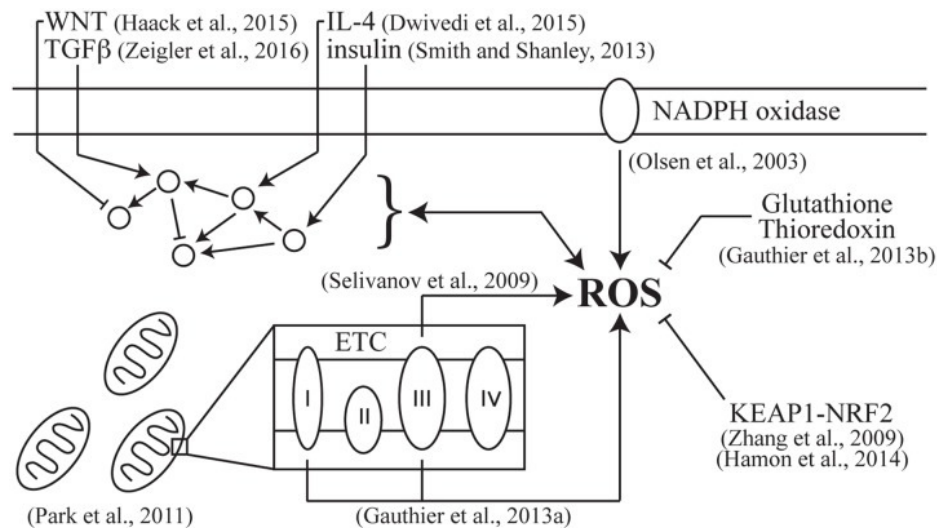
| Time-dependent variables | Differential equations                                                                                                                                                                      |
|--------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| $[P]$                    | $\frac{d[P]}{dt} = v_{ODC} + v_{PAOaD} - v_{SpdS} - v_{P_{efflux}}$                                                                                                                         |
| $[D]$                    | $\frac{d[D]}{dt} = v_{SpdS} + v_{PAOaD} - v_{SpmS} - v_{SSATD}$                                                                                                                             |
| $[S]$                    | $\frac{d[S]}{dt} = v_{SpmS} - v_{SSATS}$                                                                                                                                                    |
| $[SAM]$                  | $\frac{d[SAM]}{dt} = v_{MAT} - v_{SAM}$                                                                                                                                                     |
| $[A]$                    | $\frac{d[A]}{dt} = v_{SAMdc} - v_{SpdS} - v_{SpmS}$                                                                                                                                         |
| $[aD]$                   | $\frac{d[aD]}{dt} = v_{SSATD} - v_{PAOaD} - v_{aD_{efflux}}$                                                                                                                                |
| $[aS]$                   | $\frac{d[aS]}{dt} = v_{SSATS} - v_{PAOaS}$                                                                                                                                                  |
| $[acCoA]$                | $\frac{d[acCoA]}{dt} = v_{acCoA} - v_{CoA} - v_{SSATS} - v_{SSATD}$                                                                                                                         |
| $[CoA]$                  | $\frac{d[CoA]}{dt} = v_{CoA} + v_{SSATS} + v_{SSATD} - v_{acCoA}$                                                                                                                           |
| $V_{ODC}^{max}$          | $\frac{dV_{ODC}^{max}}{dt} = k_s^{ODC} \left( \frac{1}{1 + (K_{eq}^{ODC} ([D] + [S]))} \right) - k_d^{ODC} \cdot Antz \cdot V_{ODC}^{max}$                                                  |
| $Antz$                   | $\frac{dAntz}{dt} = k_s^{Antz} \left( 1 - \frac{1}{1 + K_{eq}^{Antz} ([D] + [S])} \right) - k_d^{Antz} \cdot Antz$                                                                          |
| $V_{SAMdc}^{max}$        | $\frac{dV_{SAMdc}^{max}}{dt} = k_s^{SAMdc} \left( \frac{1}{1 + (K_{eq}^{SAMdc} ([D] + [S]))} \right) - k_d^{SAMdc} \cdot V_{SAMdc}^{max}$                                                   |
| $V_{SSAT}^{max}$         | $\frac{dV_{SSAT}^{max}}{dt} = k_s^{SSAT} \left( 1 - \frac{1}{1 + (K_{eq}^{SSAT} ([D] + [S]))} \right) - k_d^{SSAT} \left( \frac{1}{1 + (K_{eq}^{SSAT} ([D] + [S]))} \right) V_{SSAT}^{max}$ |

## 5. Metionino ciklo modelis



6. Saa PA, Nielsen LK. Construction of feasible and accurate kinetic models of metabolism: **A Bayesian approach**. Sci Rep. 2016 Jul 15;6:29635. doi: 10.1038/srep29635. PMID: 27417285; PMCID: PMC4945864.

## 6. ROS – reaktyvių radikalų modeliavimas

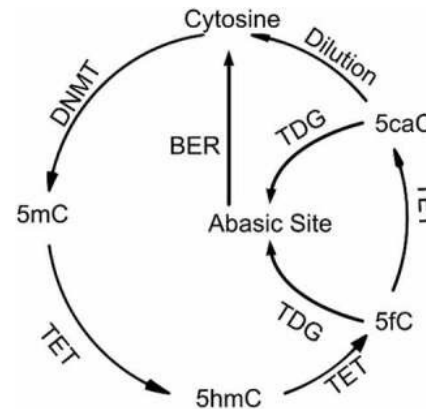


7. Pereira EJ, Smolko CM, Janes KA. **Computational Models** of Reactive Oxygen Species as Metabolic Byproducts and Signal-Transduction Modulators. Front Pharmacol. 2016 Nov 29;7:457. doi: 10.3389/fphar.2016.00457. PMID: 27965578; PMCID: PMC5126069.

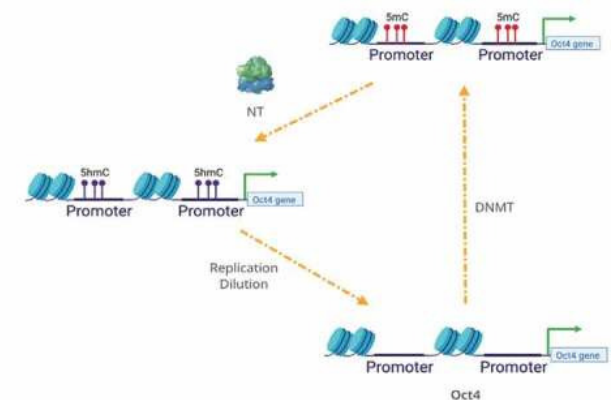
## 7. DNR metilnimo modeliavimas

The reduced dynamical system's ODEs can be written as below:

$$\begin{aligned} \frac{dN}{dt} &= m_1 - \delta N + \alpha_N O (K_O + O), \\ \frac{dT}{dt} &= m_2 - \delta T + \alpha_T N T O (N T + K_{NT} K_d) (K_O + O), \\ \frac{dO}{dt} &= -K_{NT} K_d \delta O - \delta N T O + K_O K_{NT} K_d m_3 + \alpha_O N T O + K_{NT} K_d m_3 O (N T + K_{NT} K_d) (K_O + O) \\ &\quad + K_O m_3 N T + m_3 N T O - K_O \delta N T O - K_O K_{NT} K_d \delta O - \alpha_O D_m N T O (N T + K_{NT} K_d) (K_O + O) \\ \frac{dD_m}{dt} &= -K_O K_{NT} K_d \gamma D_m + K_O K_{NT} K_d \gamma - \theta K_O N_2 T_2 D_m - \theta N_2 T_2 O D_m K_d (N T + K_{NT} K_d) (K_O + O) \\ &\quad - \theta K_O K_{NT} K_d N T D_m + \theta K_{NT} K_d N T O D_m K_d (N T + K_{NT} K_d) (K_O + O) \end{aligned}$$



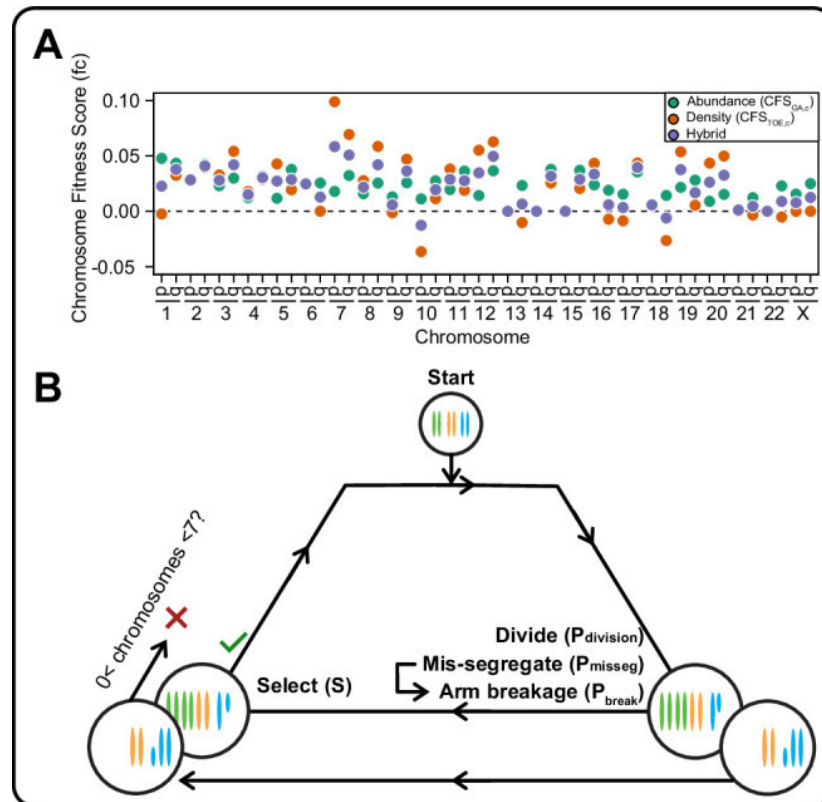
a. TET-Mediated Demethylation



b. Demethylation as a triangle topology

8. Chen T, Ali Al-Radhawi M, Sontag ED. **A mathematical model** exhibiting the effect of DNA methylation on the stability boundary in cell-fate networks. Epigenetics. 2021 Apr;16(4):436-457. doi: 10.1080/15592294.2020.1805686. Epub 2020 Sep 22. PMID: 32842865; PMCID: PMC7993226.

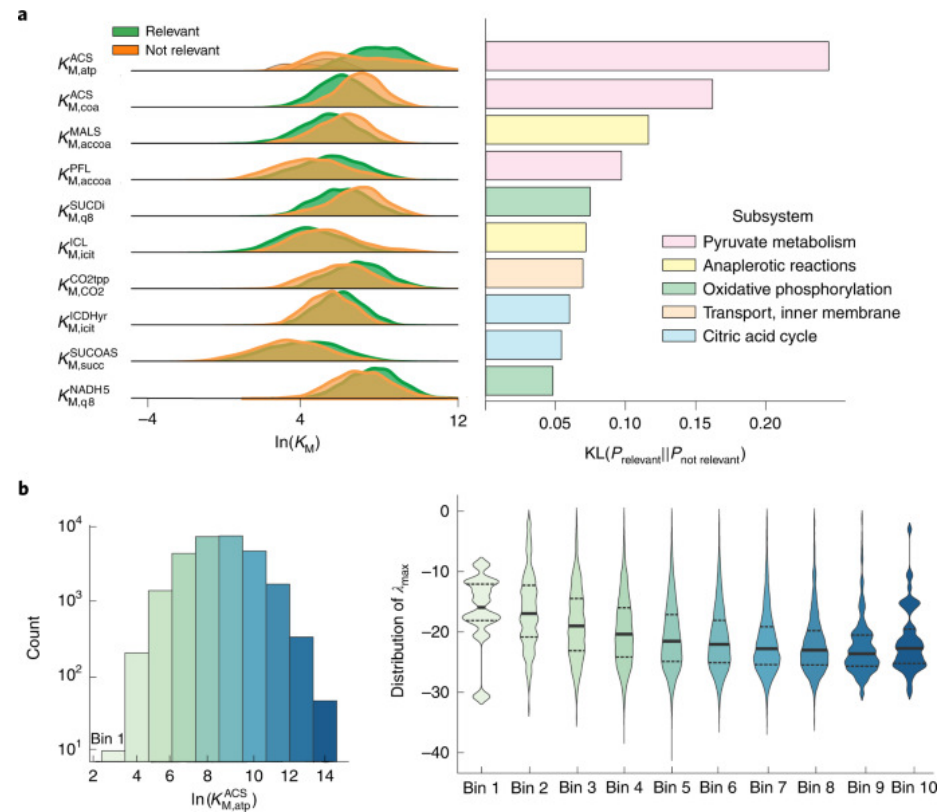
## 8. Chromosomų nestabilumo modeliavimas



9. Lynch AR, Arp NL, Zhou AS, Weaver BA, Burkard ME. Quantifying chromosomal instability from intratumoral karyotype diversity using agent-based modeling and Bayesian inference. *Elife*. 2022 Apr 5;11:e69799. doi: 10.7554/eLife.69799. PMID: 35380536; PMCID: PMC9054132.

# Dirbtinis intelektas kinetinių modelių generavimui

Reconstructing Kinetic Models for Dynamical Studies of Metabolism using Generative Adversarial Networks, Nature Machine Intelligence volume 4, pages 710–719 (2022)



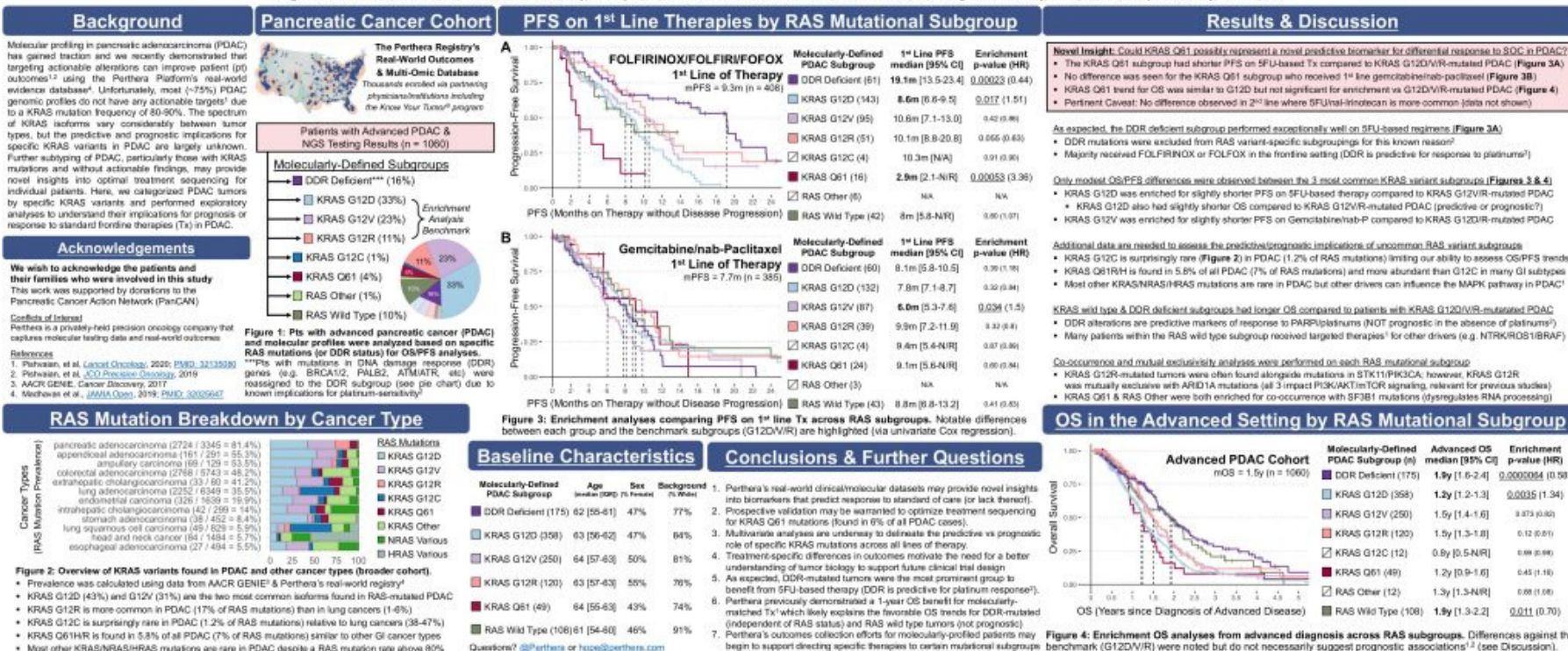
# Perthera

The Precision Oncology Outcomes Company



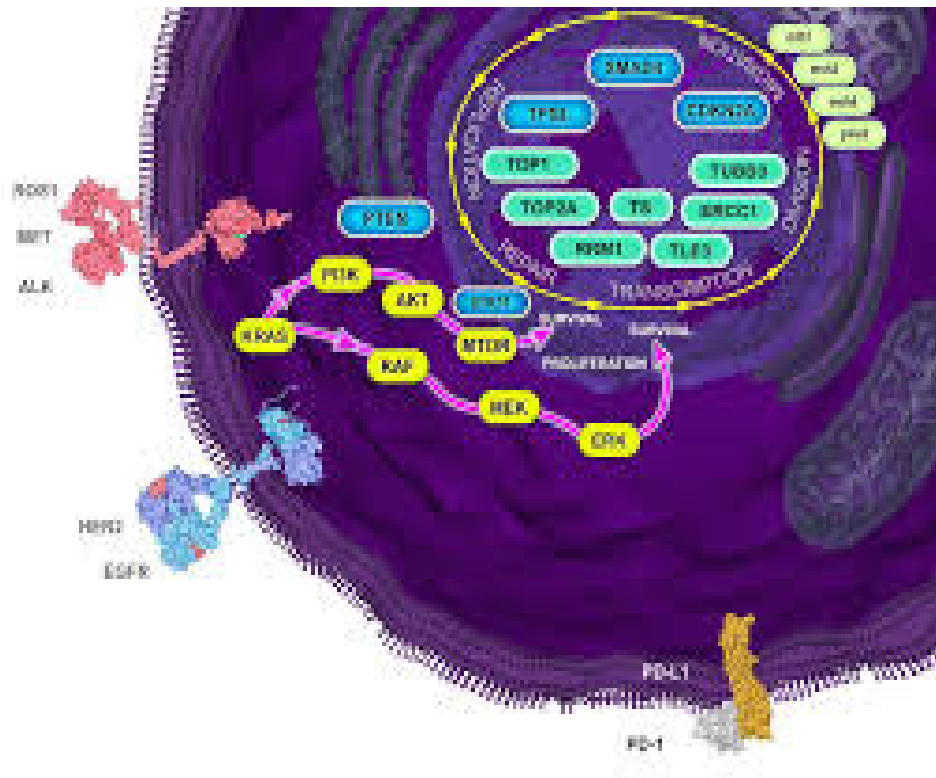
## Comprehensive analysis of KRAS variants in patients (pts) with pancreatic cancer Clinical/molecular correlations and real-world outcomes across standard therapies

Andrew E Hendifar<sup>1</sup>, Edik M Blais<sup>2</sup>, Camille Ng<sup>3</sup>, Dzung Thach<sup>2</sup>, Jun Gong<sup>1</sup>, Davendra Sohail<sup>3</sup>, Vincent Chung<sup>1</sup>, Vaibhav Sahai<sup>3</sup>, Christos Fountzilas<sup>4</sup>, Samah Mikhail<sup>1</sup>, Gary L Gregory<sup>5</sup>, Jonathan R Brody<sup>6</sup>, Emily Lyons<sup>7</sup>, Patricia DeArbela<sup>8</sup>, Lynn M Matrisian<sup>9</sup>, Emanuel F Petricoin III<sup>10</sup>, Michael J Pishvaian<sup>2,11</sup>  
<sup>1</sup>Cedars-Sinai Medical Center, Los Angeles, CA; <sup>2</sup>Perthera, Inc, Holliston, MA; <sup>3</sup>Cleveland Clinic, Cleveland, OH; <sup>4</sup>City of Hope Cancer Center, Duarte, CA; <sup>5</sup>University of Michigan, Ann Arbor, MI; <sup>6</sup>Roswell Park Cancer Institute, Buffalo, NY; <sup>7</sup>Zangmeister Cancer Center, Columbus, OH; <sup>8</sup>Thomas Jefferson University, Philadelphia, PA; <sup>9</sup>The Pancreatic Cancer Action Network, Manhattan Beach, CA; <sup>10</sup>George Mason University, Fairfax, VA; <sup>11</sup>Johns Hopkins University, Baltimore, MD



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The Precision Oncology Outcomes Company



# TUMORIGENEZĖ

K-RAS PROBLEMA ONKOLOGIJOJE: SISTEMINIS POŽIŪRIS

**Kęstutis K.Urba**

**VILNIUS 2025**

## TURINYS

### Įvadas

- I. Hanahan-Weinberg vėžio modelio patikslinimas ir Warburgo bei Hofmano efektai bei formalus vėžio aprašas
- II. K-ras mutacijos, signaliniai keliai, biologinės funkcijos
- III. Vienanglių fragmentų apykaita vėžio ląstelėse ir K-RAS
- IV. Epigenetinių DNR metilinimo pokyčių modelis – hepatokarcinoma
- V. K-RAS ir poliaminų apykaita piktybinėje ląstelėje bei sąryšis su Metionino ciklo ypatumais
- VI. K-RAS ir metaloproteinazės, adamlizinais, tarpląstelinės ir matrikso jungtys, angiogenezė, imunitetas
- VII. Epigenetiniai chromosomų stabilumo, DNR metilinimo, histonų pokyčiai piktybinėje ląstelėje ir K-RAS
- VIII. K-RAS mutacijos ir ląstelės ciklas
- IX. Cholangiokarcinomos
- X. Skrandžio vėžys
- XI. K-ras mutacijos ir kasos, žarnyno, plaučių vėžys
- XII. Kasos navikai
- XIII. Kolorektaliniai navikai
- XIV. Plaučių navikai
- XV. Prostatos vėžys
- XVI. Melanoma ir K- RAS mutacijos
- XVII. Poveikio genai, K-RAS ir vėžio heterogeniškumas
- XVIII. Kancerogenezės teorijos, koncepcijos, aiškinimai
- XIX. K-ras mutacijų sąlygoti kancerogenezės scenarijai
- XX. *Imuninė sistema ir K-ras*
- XXI. Kompleksinė sisteminė adaptivi orientuota į mK-RAS ir jo betarpišką metabolinę aplinką neo-adjuvantinė bei adjuvantinė medikamentinė taikinių terapija
- XXII. Kiekybiniai matematiniai modeliai onkologijoje

LITERATŪRA – apie 1500 publikacijų

Europe's Beating Cancer Plan will be implemented,  
enabled and supported using the whole range of  
Commission funding instruments  
with a total of €4 billion



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## Europe's beating cancer plan

#EUCancerPlan #HealthUnion



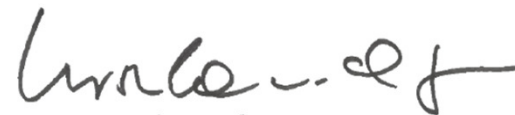
# Ursulos von der Leyen palaiminimas Lietuvai

*I have passed your report on to my colleagues across the Commission who are working on the development of a comprehensive EU Cancer Plan that will include actions across the entire disease pathway: prevention, early detection and diagnosis, treatment, quality of life as a cancer survivor and palliative care. The proposed actions will aim to ensure that all Europeans will have access to effective prevention and care, respecting the principles of proportionality and subsidiarity.*

*Currently the Commission is consulting with stakeholders on the potential content and scope of the EU Cancer Plan. Your contribution to the discussion is much appreciated, and your emphasis on prevention, more knowledge, inequities, innovation and avoiding stigmatisation are well noted.*

*I wish to take this opportunity to thank you for your personal contribution and active role in public health in general and fighting cancer in particular. In times like these, Europe needs health advocates like you and I count on your continued cooperation and involvement in making Europe better and healthier for our people. Related to this, I welcome the initiative to develop a 'Lithuanian flagship Initiative for beating cancer' and the Commission remains available for further support.*

*Yours faithfully,*



Ursula von der Leyen



# Ačiū už dėmesį!

